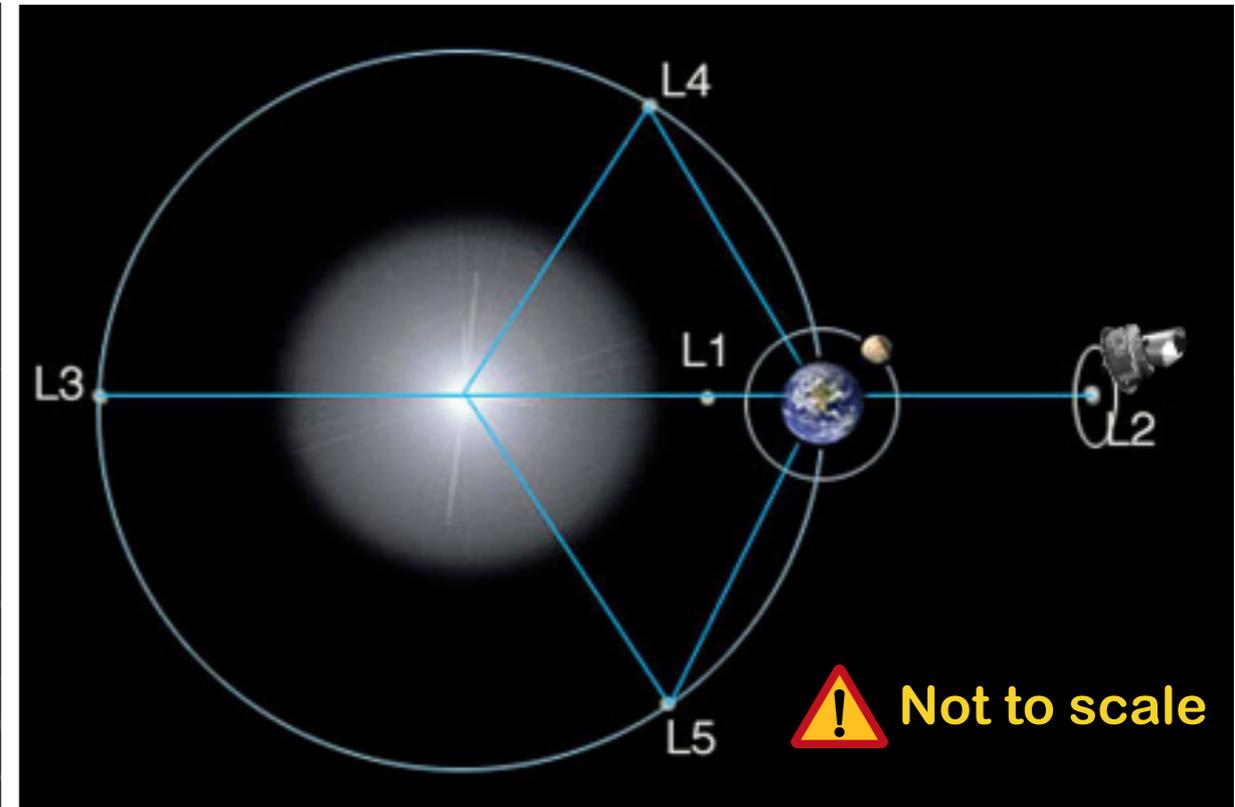
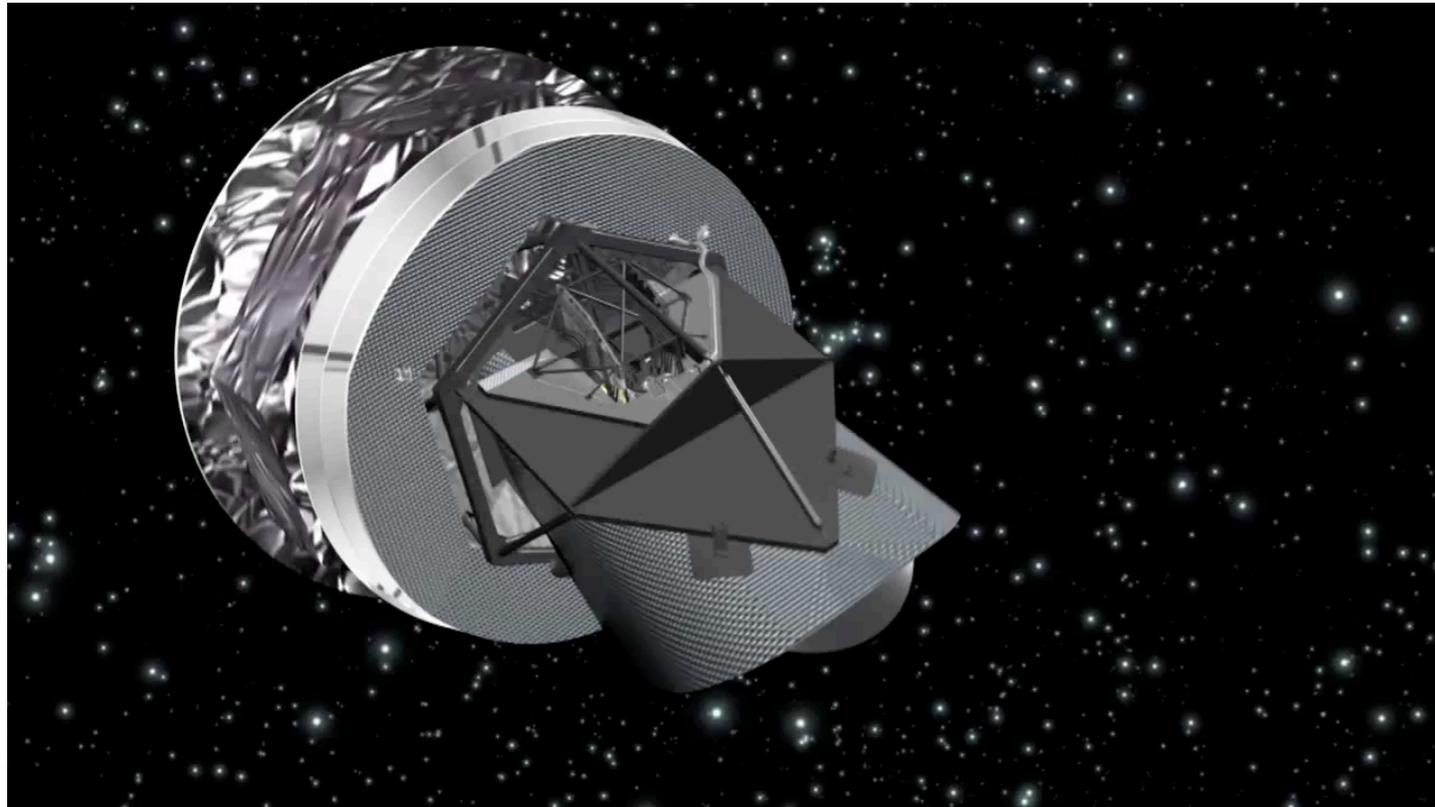


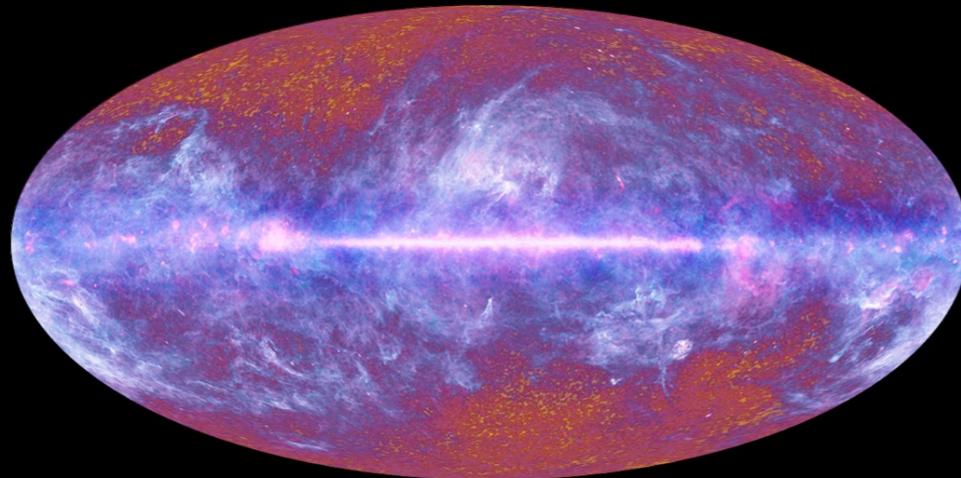
***Polarized thermal emission from Galactic dust***

# The Planck mission

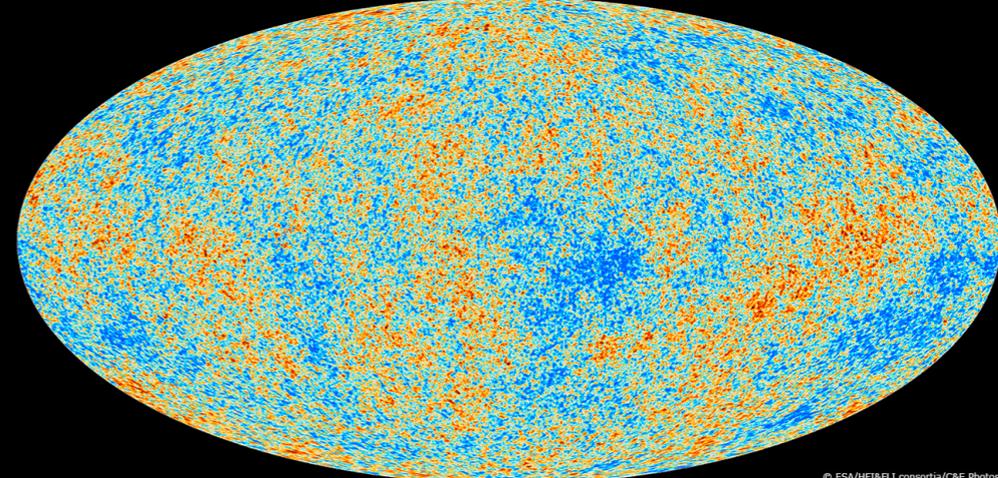


- 2009-2013 European space mission : Full survey of the microwave sky
- 30 - 857 GHz coverage in nine bands
- Measurement of Cosmic Microwave Background (CMB) anisotropies
- Mapping of the cold, dusty Milky Way
- First full-sky survey in microwave polarization

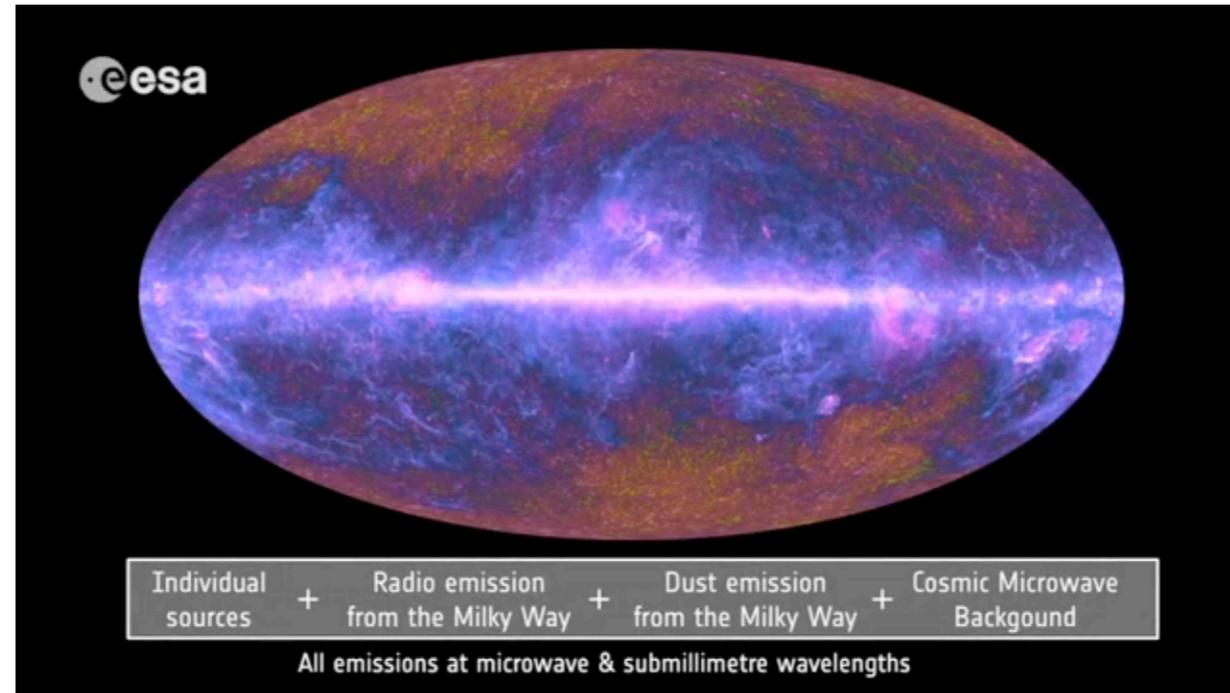
The Planck 1-year survey (2011)



The Planck CMB temperature map (2013)

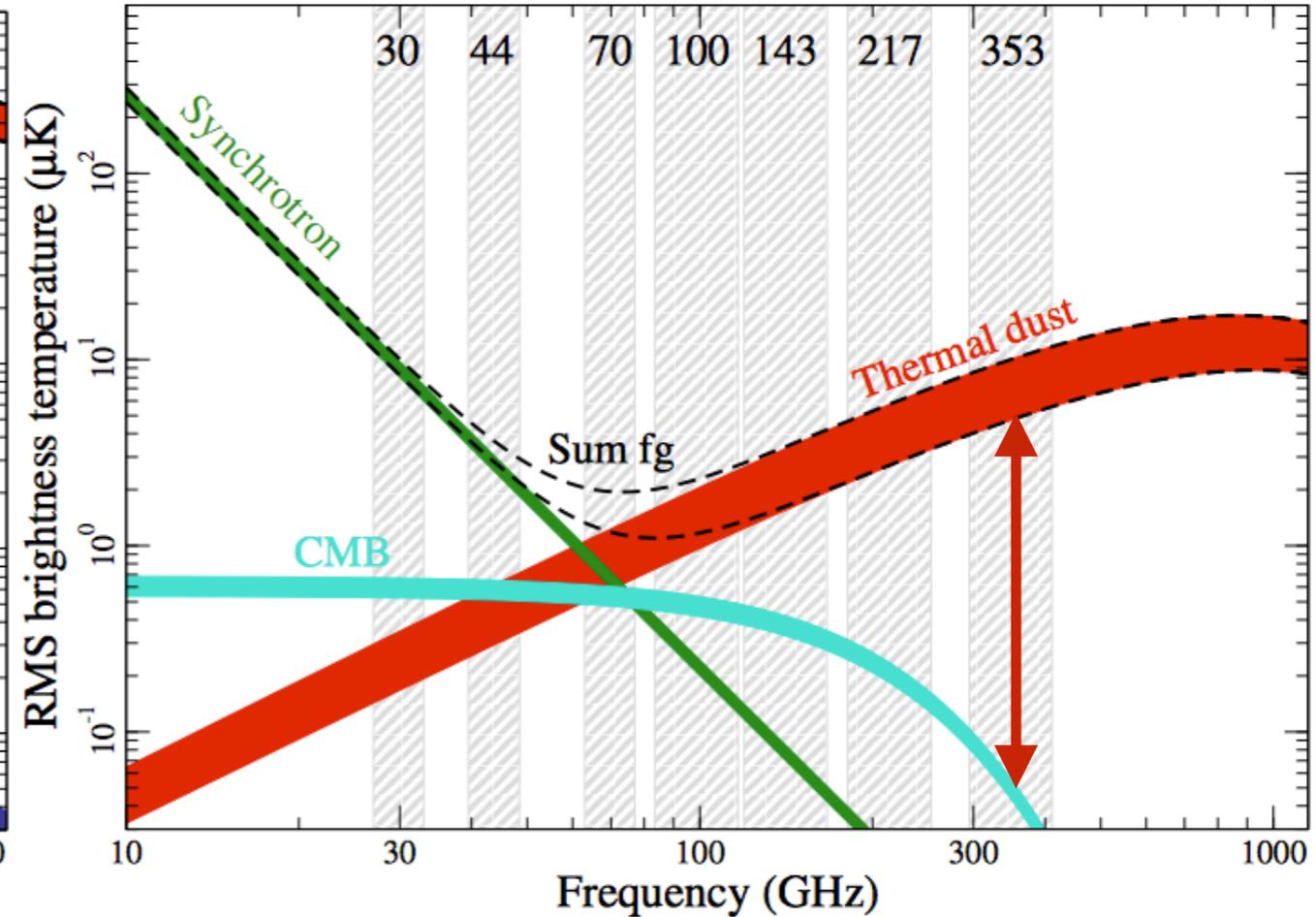
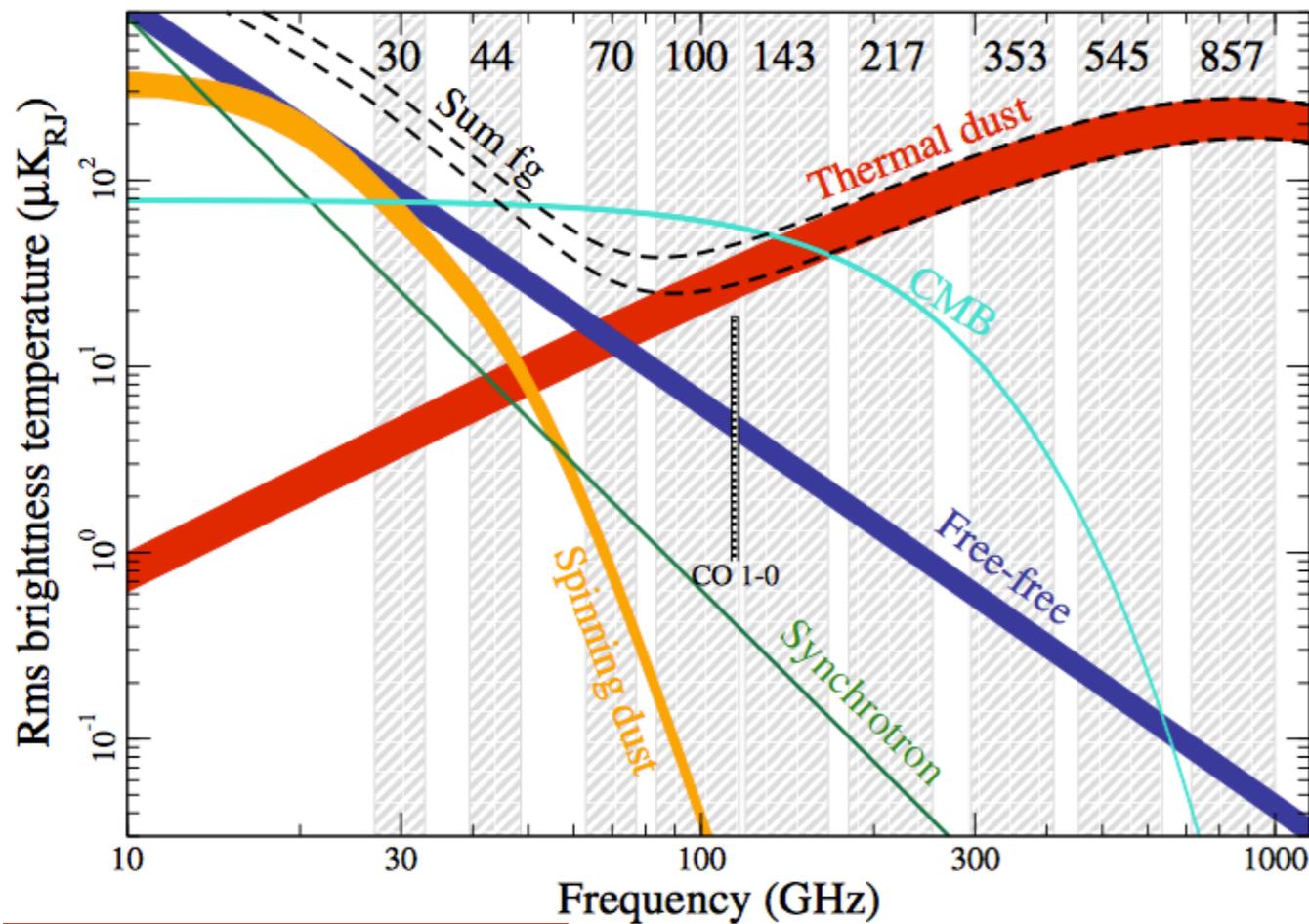


# Galactic dust emission : a foreground to the CMB



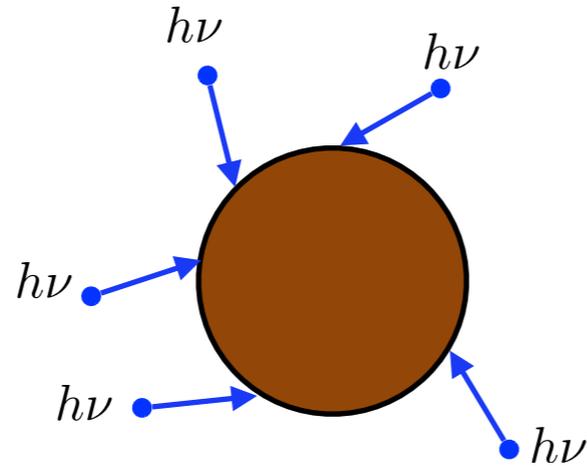
**Total intensity**

**Polarized intensity**

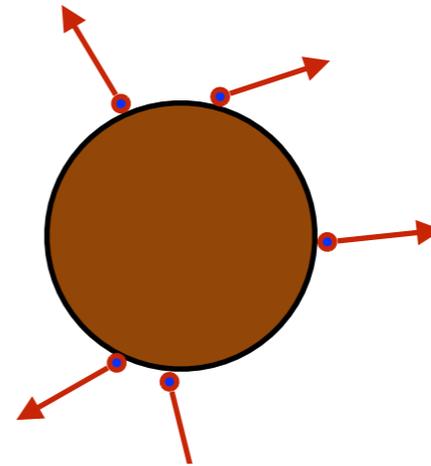


# Interstellar dust emission

UV and visible absorption



Infrared emission (~ 10 K)

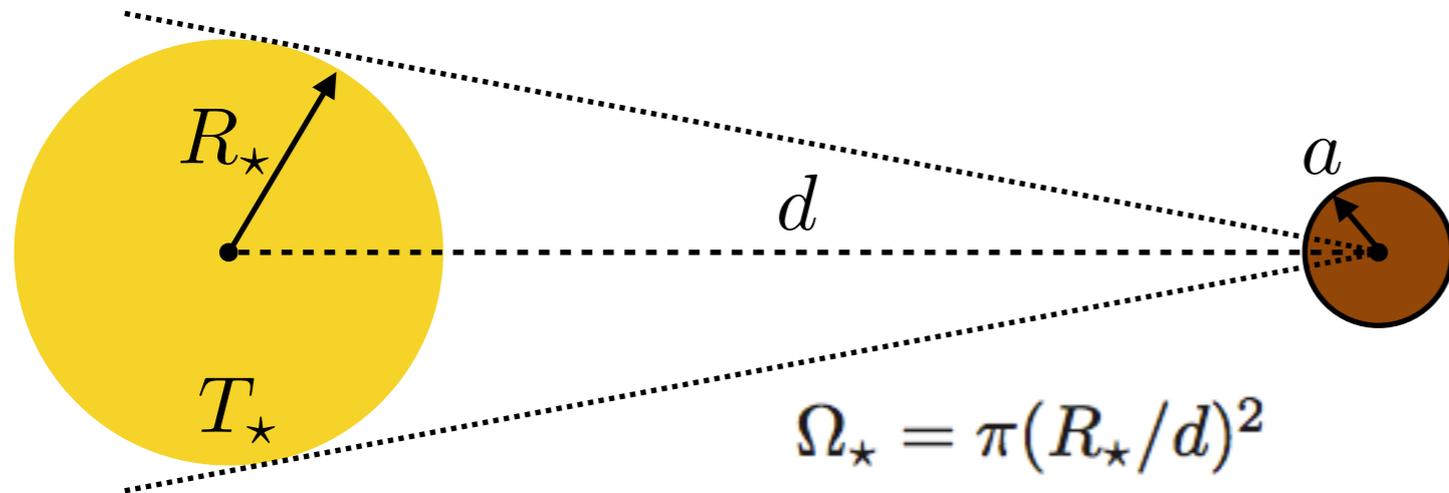


Large grains at equilibrium

$$\int \kappa_\nu J_\nu d\nu = \int \kappa_\nu B_\nu (T_d) d\nu$$

← Grain temperature

Example



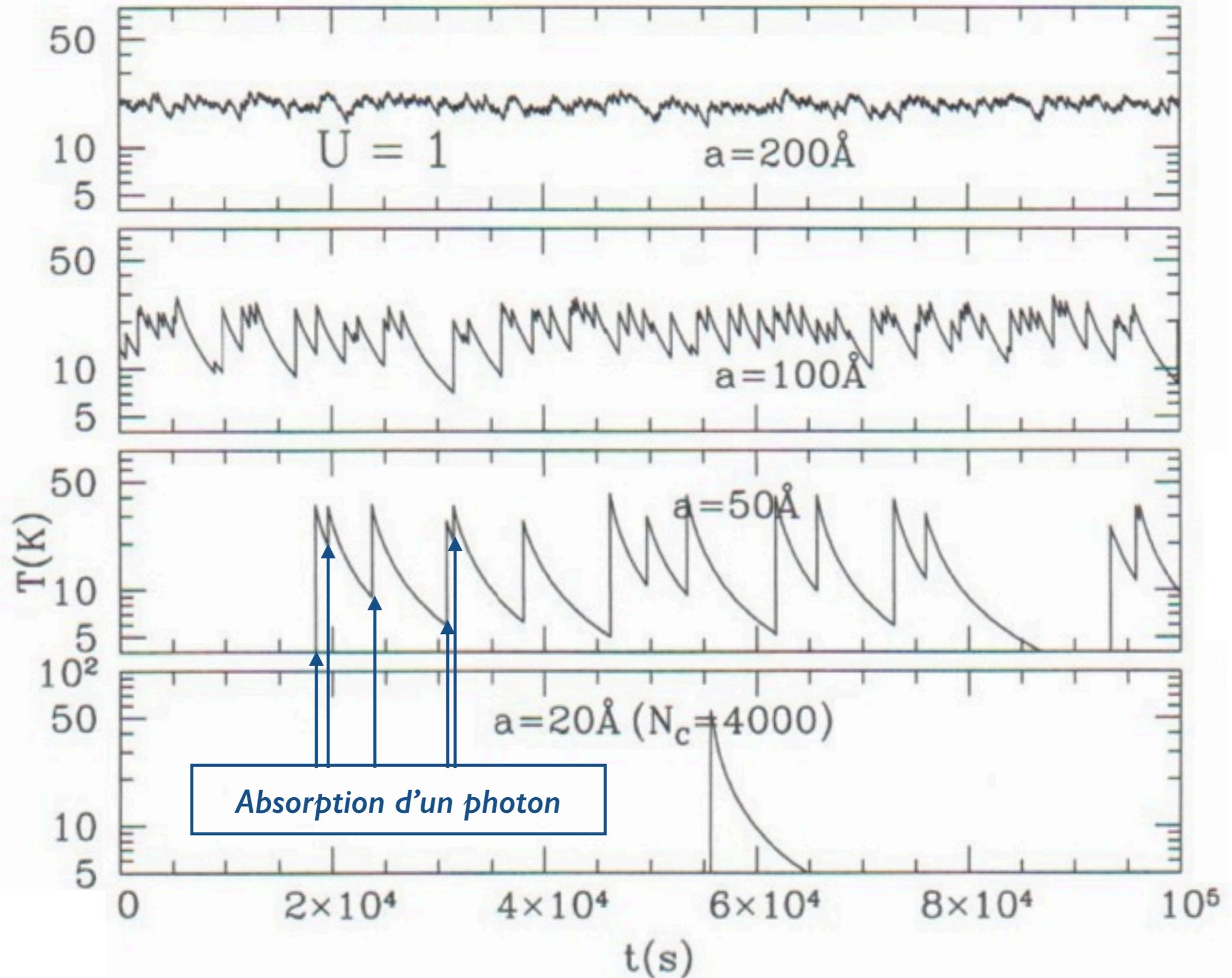
Equilibrium temperature

$$T_d = C_\beta \left[ \frac{T_\star^4}{a} \left( \frac{R_\star}{d} \right)^2 \right]^{1/(4+\beta)}$$

Spectral index in the IR  $\beta \simeq 1 - 2$

$$\delta T \sim \frac{h\nu}{C}$$

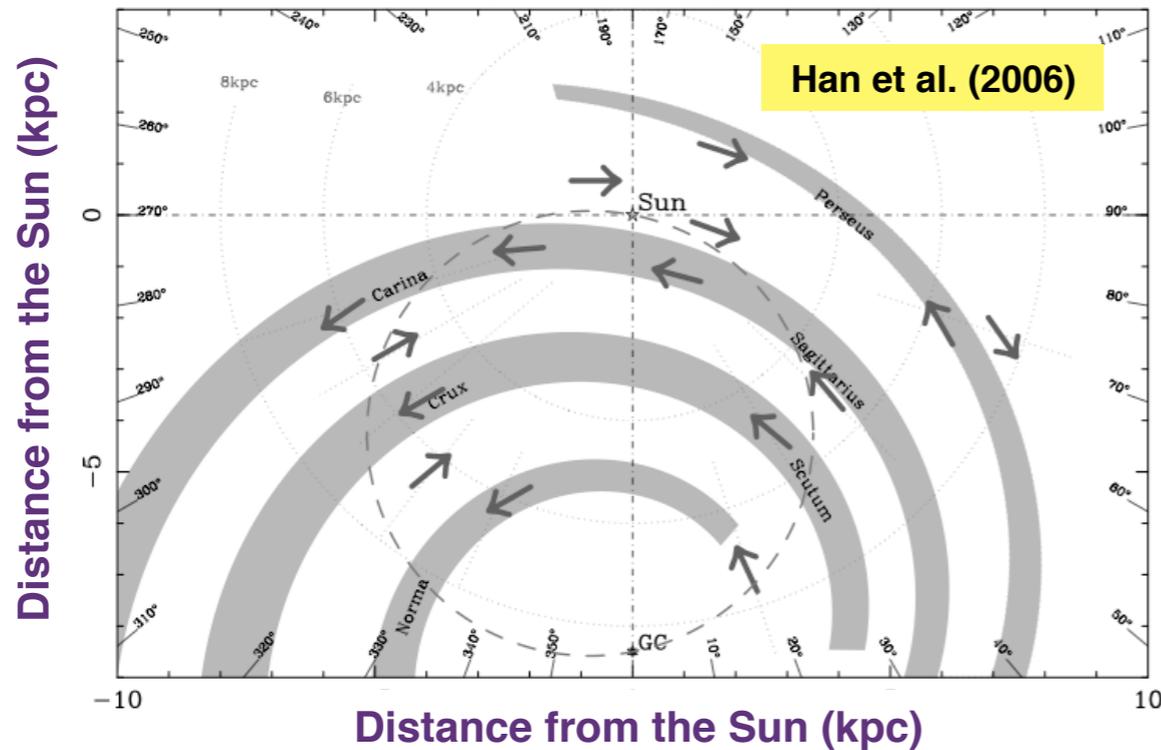
## Interstellar dust emission



# Magnetic fields in the Milky Way

- Coupled to the gas, provides balance with gravity, controls the propagation of cosmic rays
- Generated from primordial seed fields via a coupling of differential rotation and Coriolis force
- Superposition of a large-scale field following spiral arms and of a turbulent component

## Field reversals



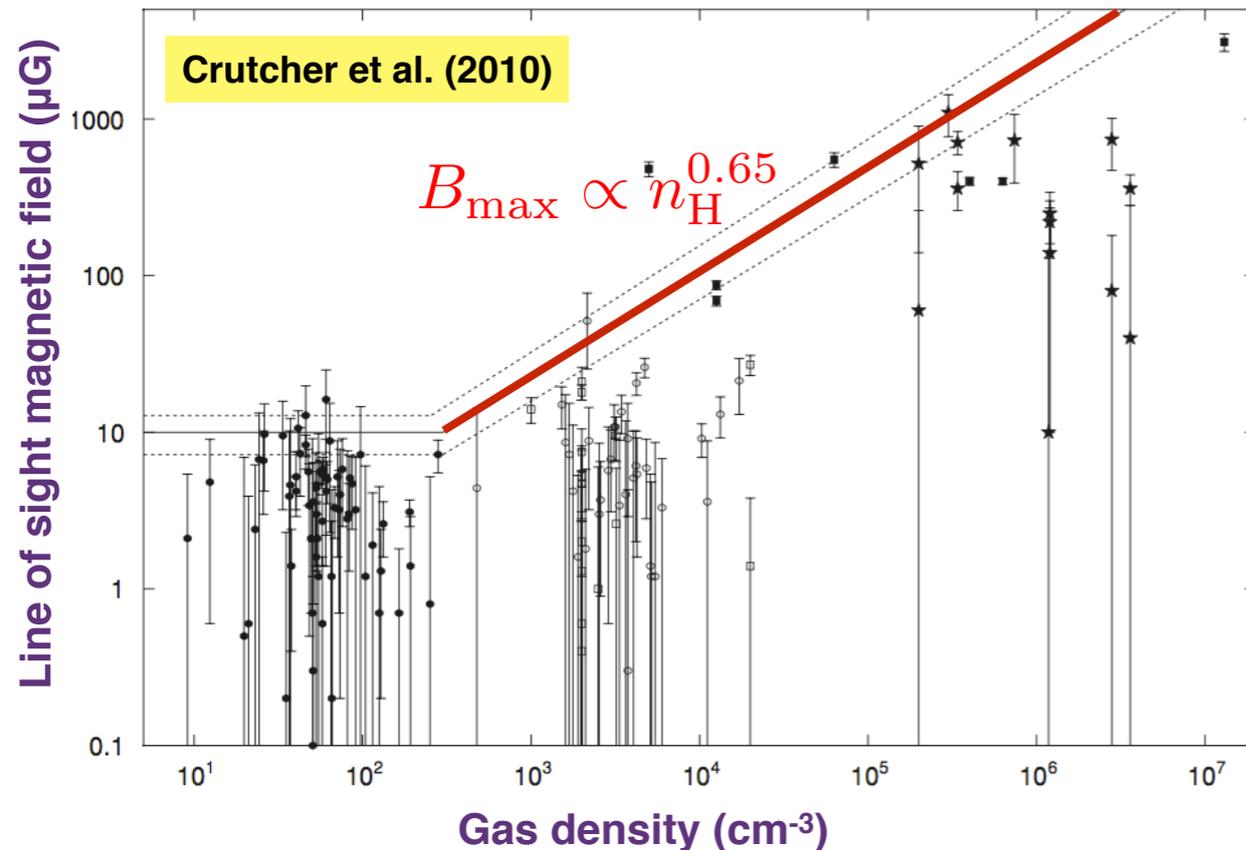
$$B = B_0 + B_t$$

$\sim$  a few  $\mu\text{G}$                        $\sim$  a few  $\mu\text{G}$

Haverkorn et al. (2008)

## Measurement methods

Notation	Observational signatures
$B_{\text{tot},\perp}^2 = B_{\text{turb},\perp}^2 + B_{\text{reg},\perp}^2$	Total synchrotron intensity
$B_{\text{turb},\perp}^2 = B_{\text{iso},\perp}^2 + B_{\text{aniso},\perp}^2$	Total synchrotron emission, partly polarized
$B_{\text{iso},\perp}$ ( $= \sqrt{2/3} B_{\text{iso}}$ )	Unpolarized synchr. intensity, beam depolarization, Faraday depolarization
$B_{\text{iso},\parallel}$ ( $= \sqrt{1/3} B_{\text{iso}}$ )	Faraday depolarization
$B_{\text{ord},\perp}^2 = B_{\text{aniso},\perp}^2 + B_{\text{reg},\perp}^2$	Intensity and vectors of radio, optical, IR & submm pol.
$B_{\text{aniso},\perp}$	Intensity and vectors of radio, optical, IR & submm pol., Faraday depolarization
$B_{\text{reg},\perp}$	Intensity and vectors of radio, optical, IR & submm pol., Goldreich-Kylafis effect
$B_{\text{reg},\parallel}$	Faraday rotation + depol., longitudinal Zeeman effect

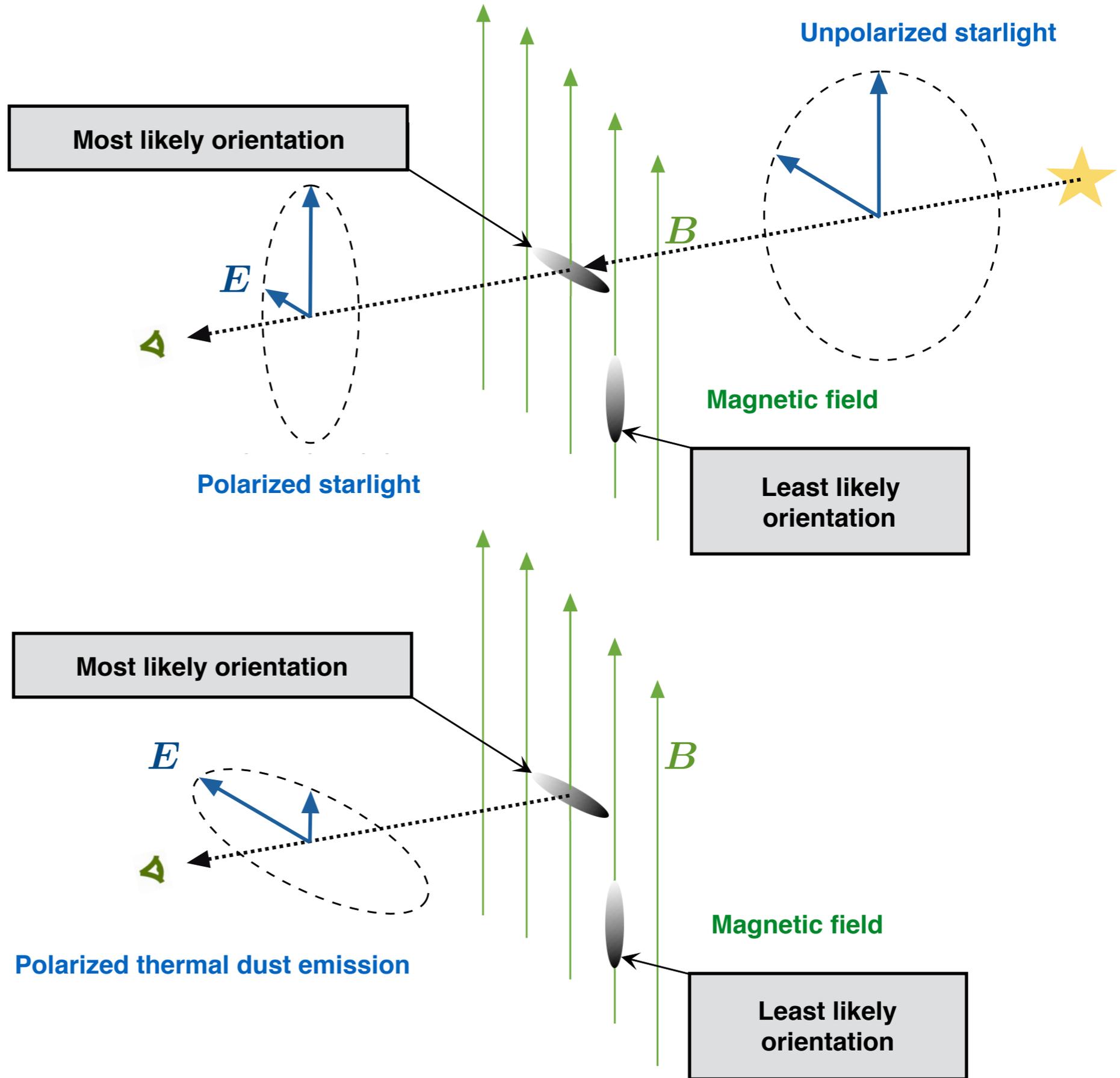
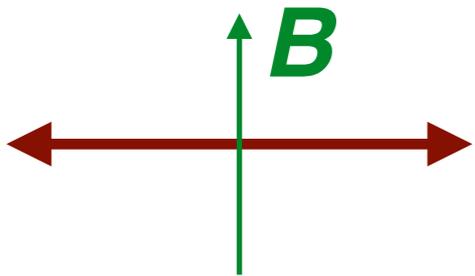


# Dust, magnetic fields and polarization

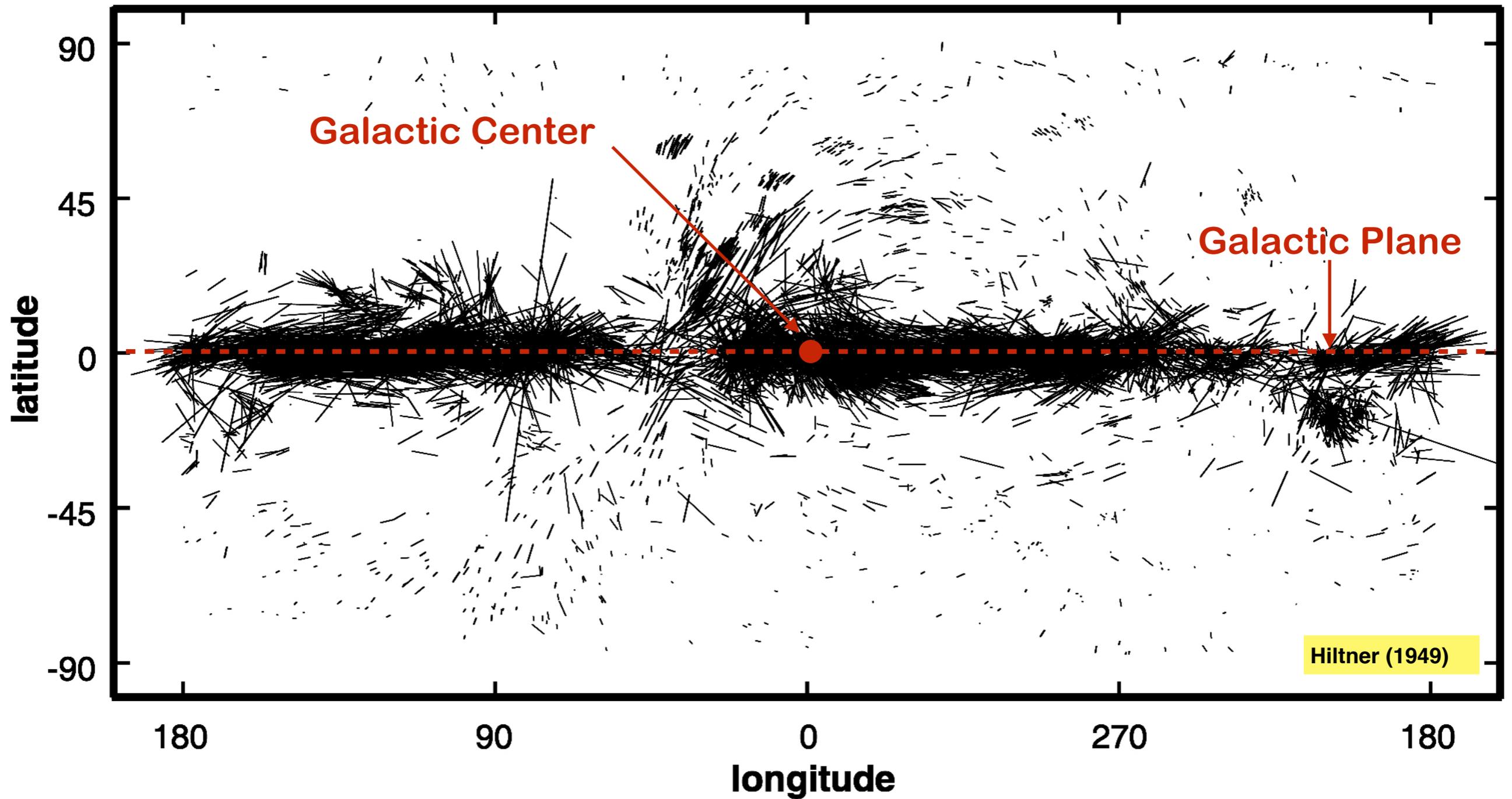
**Optical  
starlight  
polarization**



**Submillimetre  
emission  
polarization**



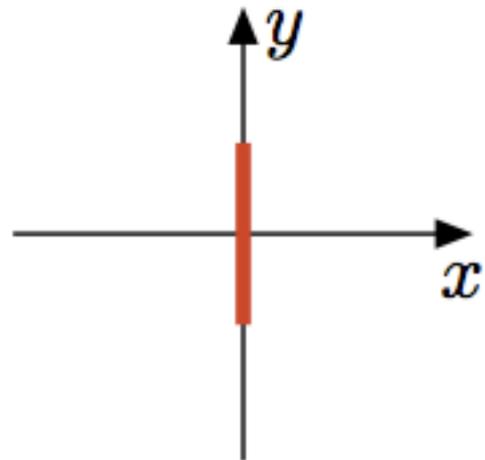
# Starlight polarisation



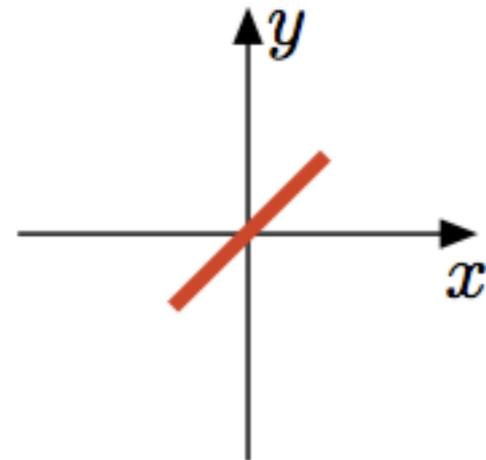
**Starlight polarization direction = Plane-of-the-sky orientation of B**

# Stokes parameters, E and B modes

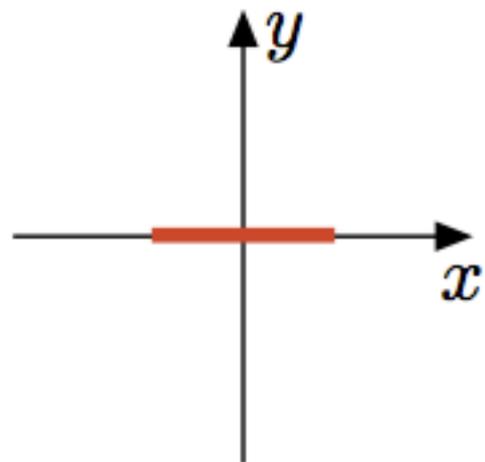
## Stokes Parameters



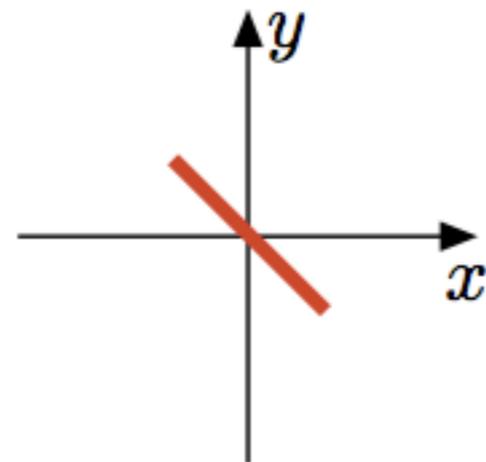
$$Q > 0, U = 0$$



$$Q = 0, U > 0$$

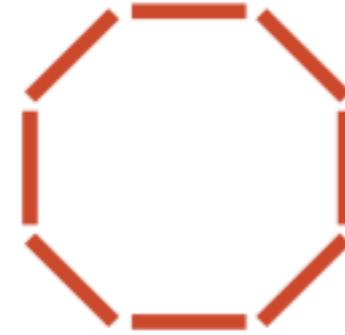


$$Q < 0, U = 0$$



$$Q = 0, U < 0$$

## E- and B-modes



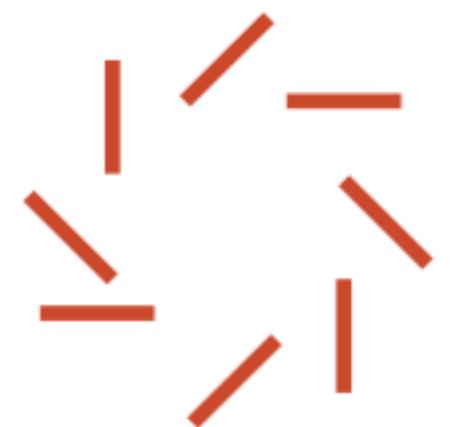
$$E > 0$$



$$E < 0$$



$$B > 0$$

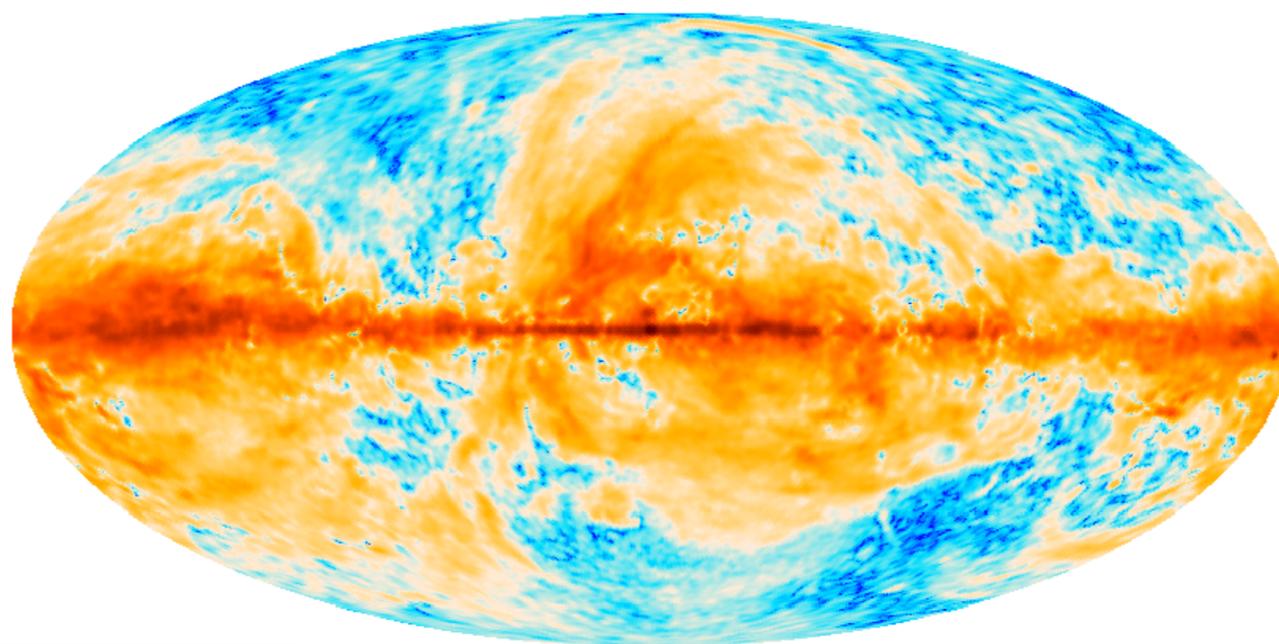
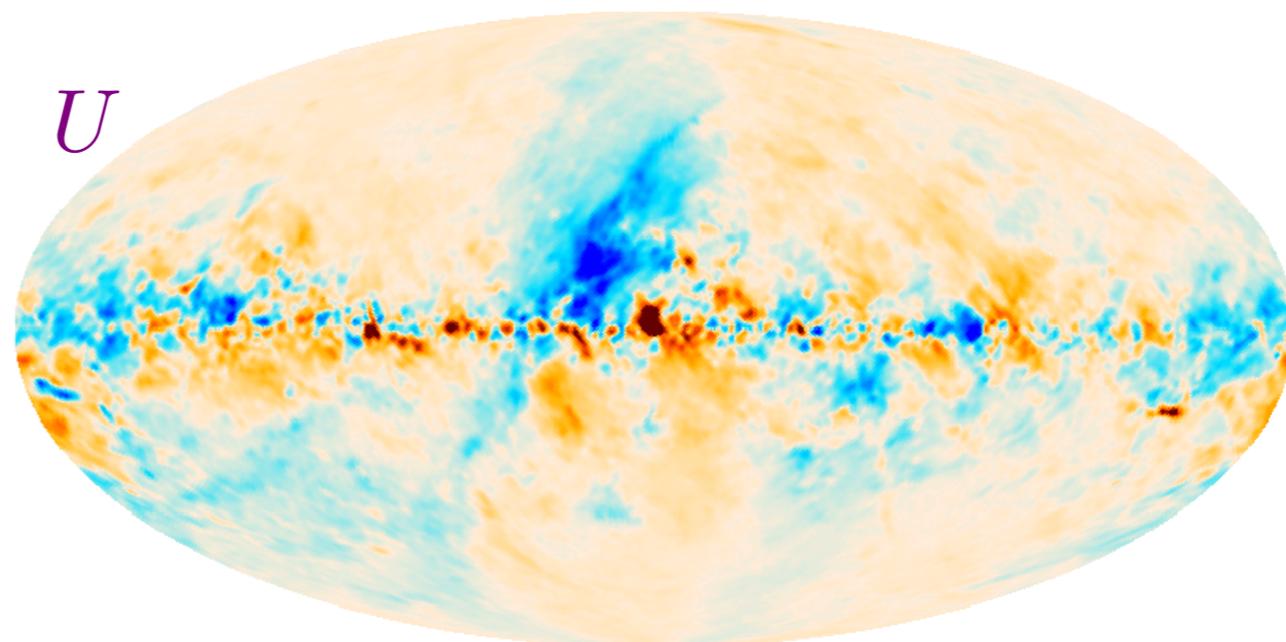
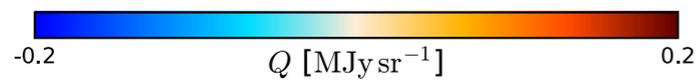
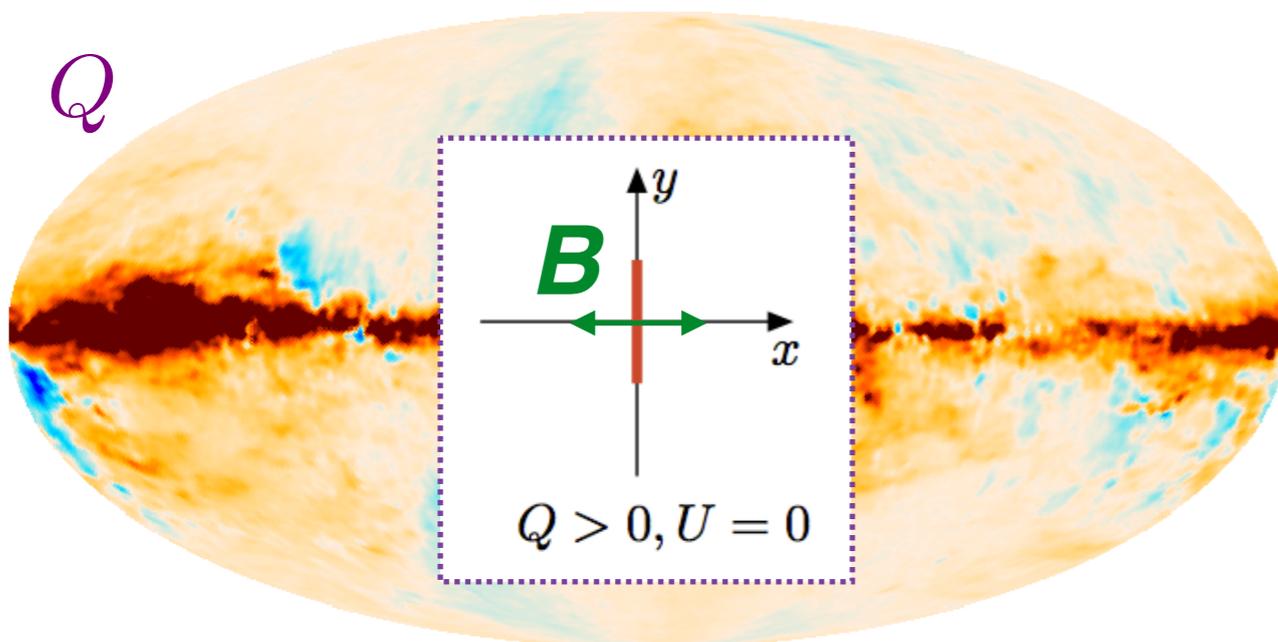


$$B < 0$$

# Polarized thermal dust emission at 353 GHz

- GNILC processing reduces noise, CMB, CIB contamination
- Maps available at varying resolution (5' to 80')
- Analysis performed on uniform 80' resolution maps

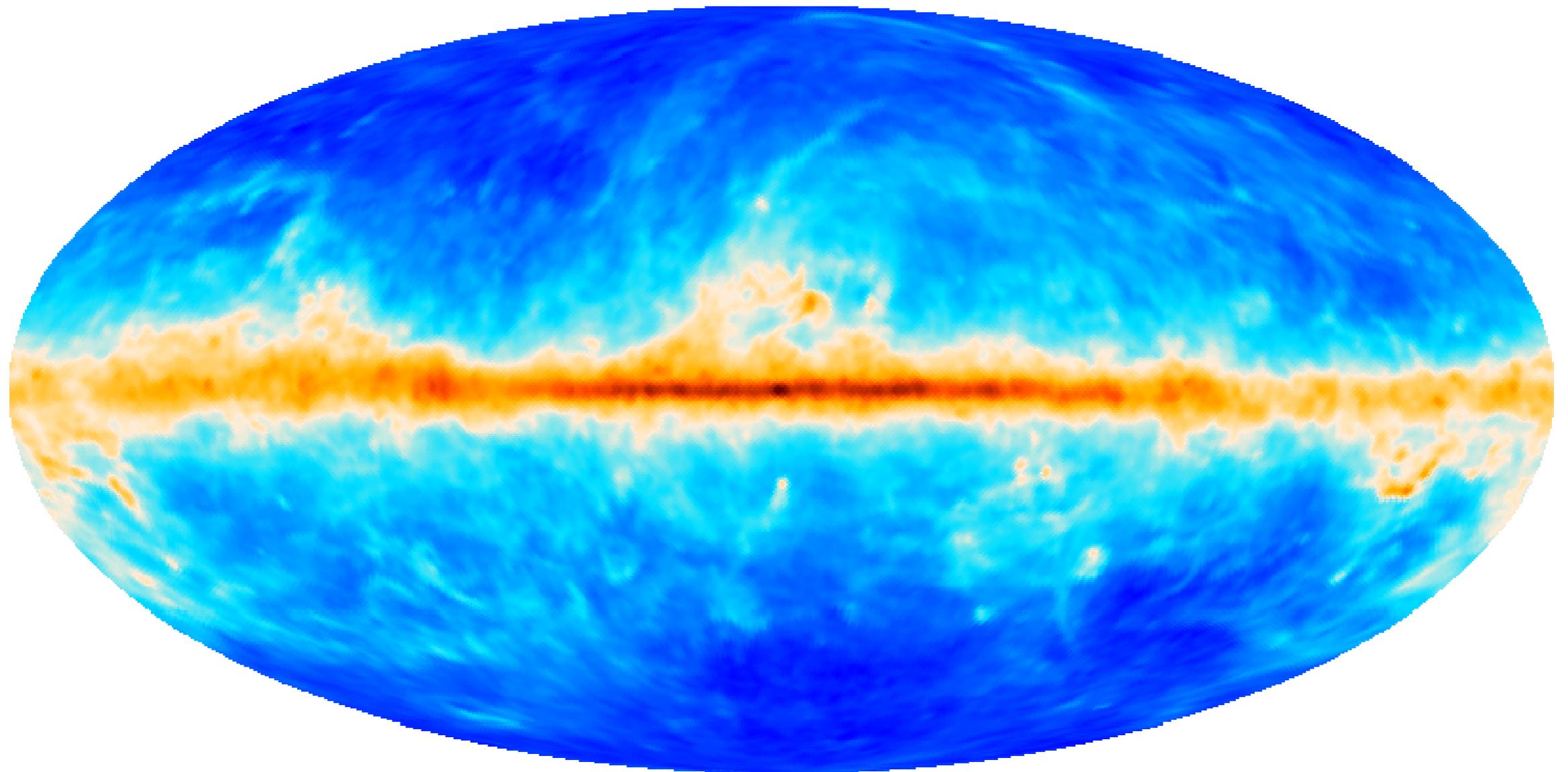
Planck Collaboration XII (in prep)  
Remazeilles et al. (2011)  
Planck Collaboration Int XLVIII (2016)



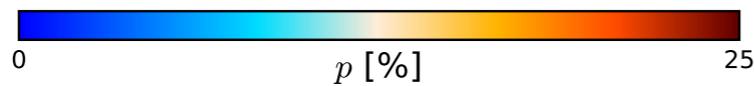
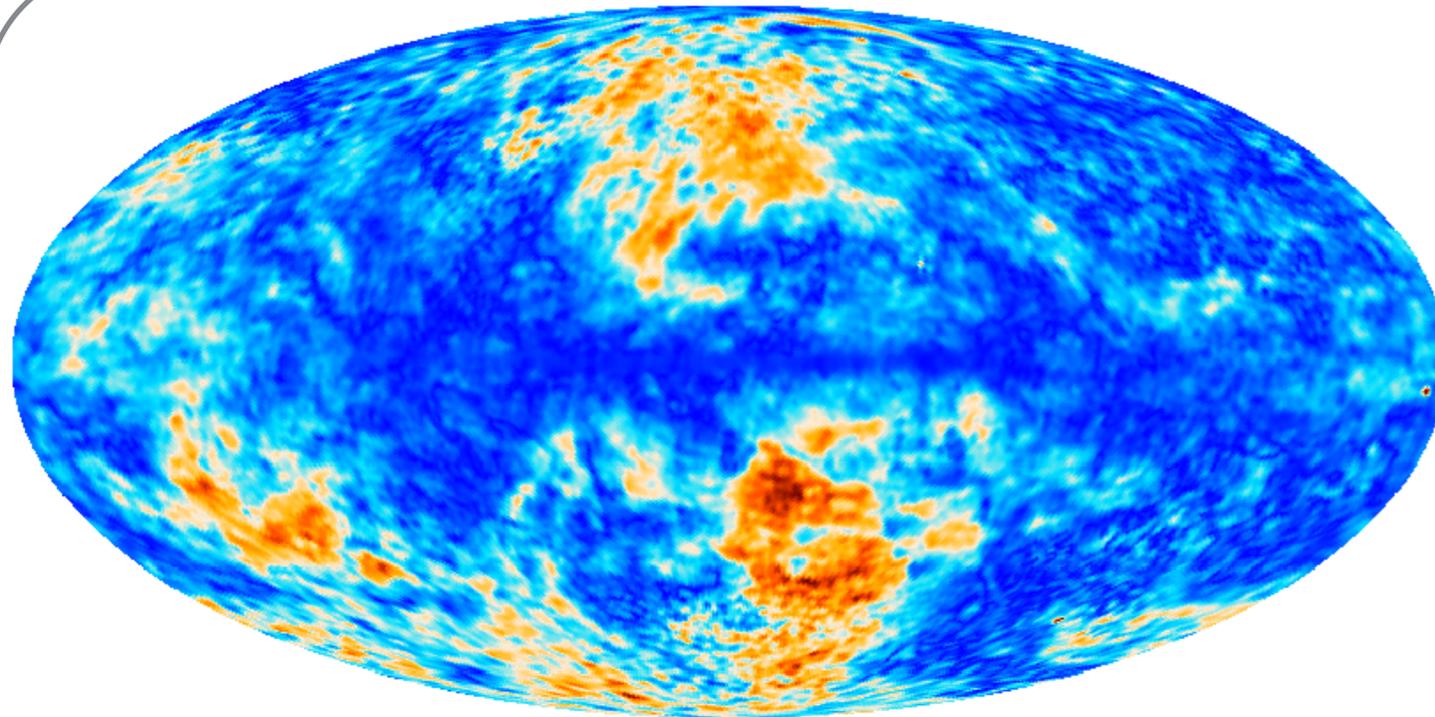
$$P = \sqrt{Q^2 + U^2}$$

-4  $\log(P/\text{MJy sr}^{-1})$  0.1

# Polarized and total intensities



# Polarization fraction and angle



## Polarization fraction

$$p = \frac{P}{I}$$

## Modified asymptotic estimator

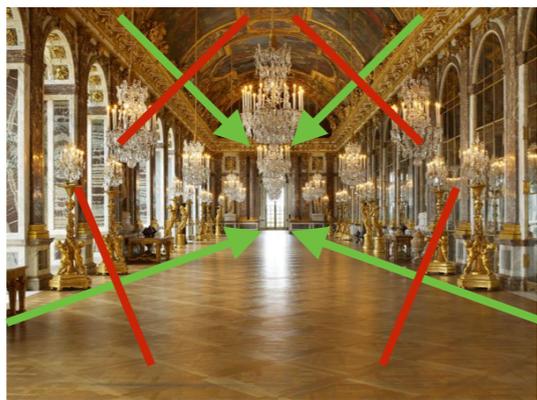
$$p_{\text{MAS}} = p - \varsigma^2 \frac{1 - e^{-p^2/\varsigma^2}}{2p}$$

Plaszczynski et al. (2014)

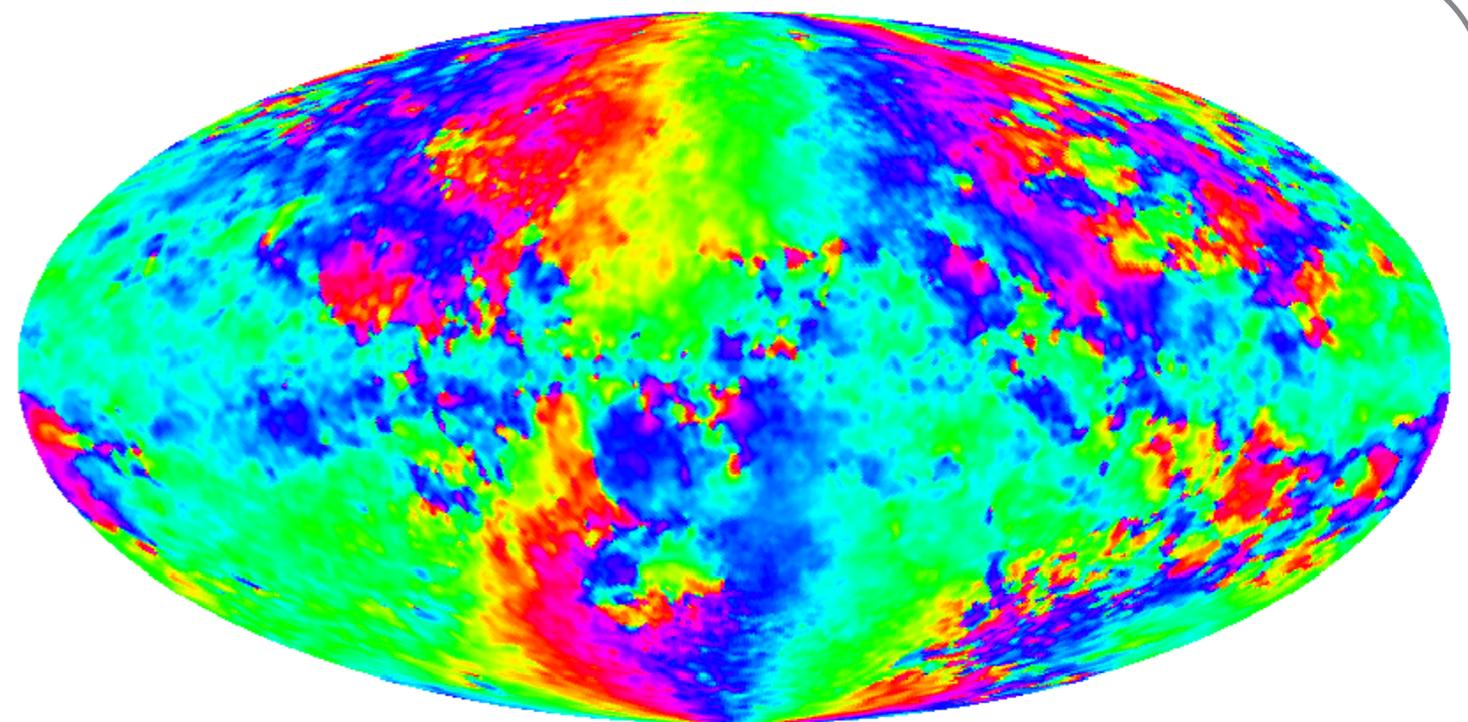
- Low polarization fractions in the Galactic Plane
- Some highly polarized regions, no material counterpart

## Polarization angle

$$\psi = \frac{1}{2} \text{atan}(-U, Q)$$



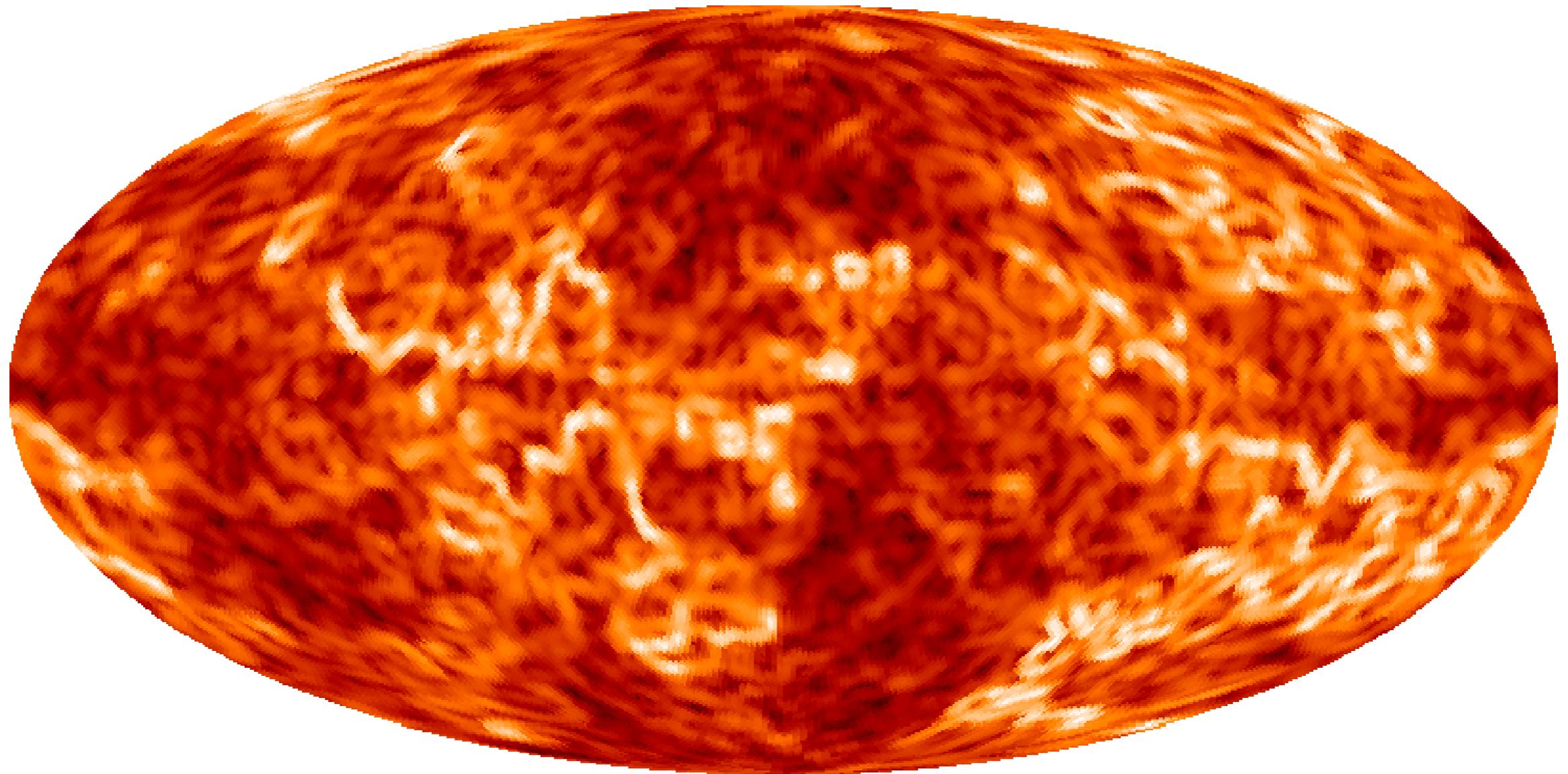
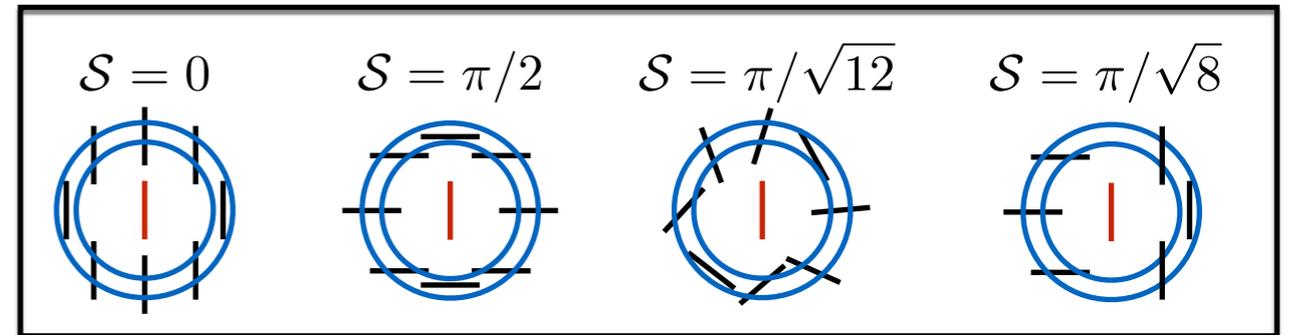
- B field along the Galactic plane
- Large-scale structure at high latitudes (see M. Alves' talk)



# Spatial structure of the polarization angle map

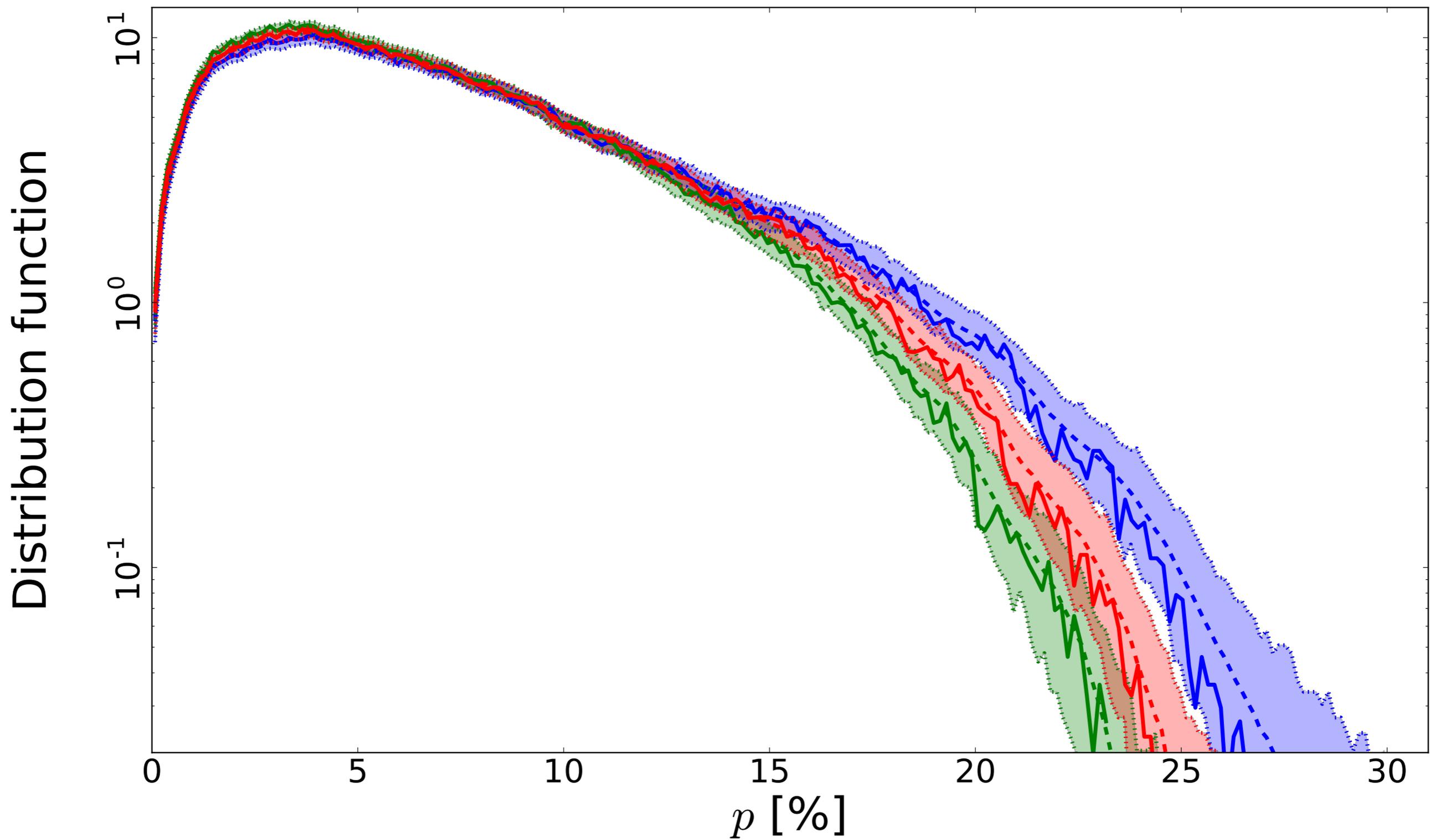
## Polarization angle dispersion function

$$\mathcal{S}(\mathbf{r}, \delta) = \sqrt{\frac{1}{N} \sum_{i=1}^N [\psi(\mathbf{r} + \delta_i) - \psi(\mathbf{r})]^2}$$



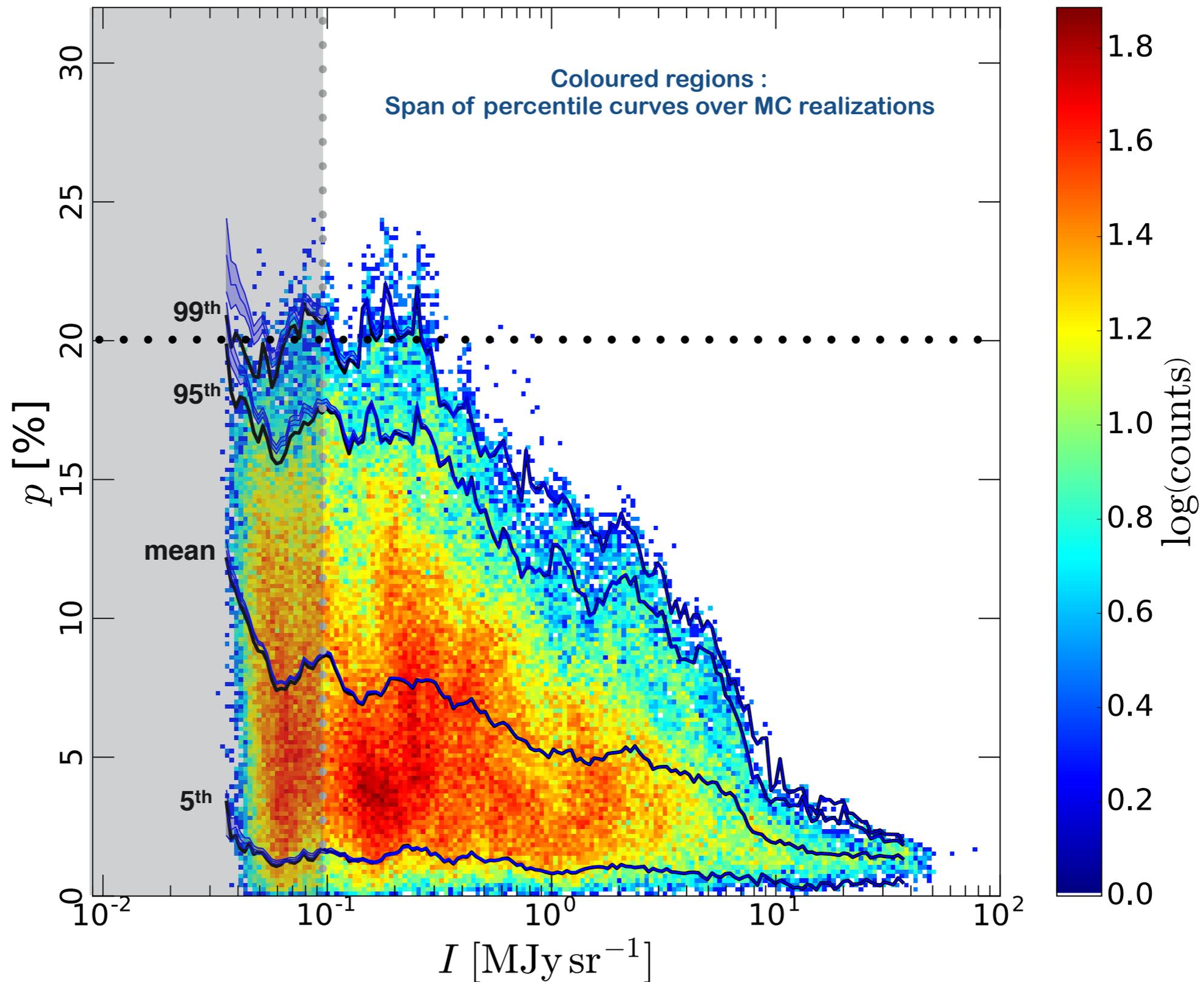
- Strongly anti-correlated with the polarization fraction
- Low  $p$  where the polarization angle direction changes abruptly

# One-point statistics of polarization fractions



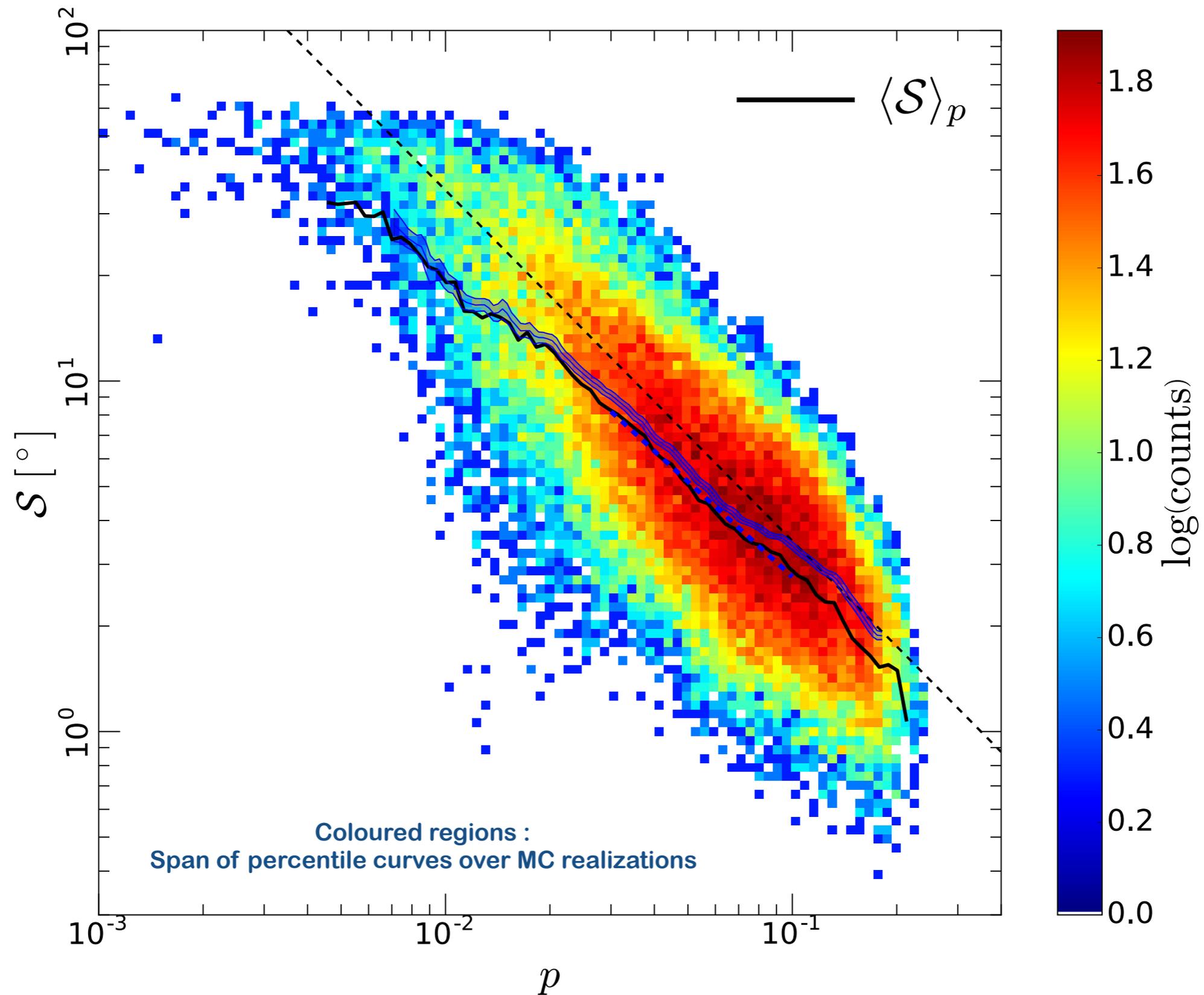
- Thick lines : data
- Coloured regions : span of DFs across a set of MC realizations
- Dotted lines : average DF across a set of MC realizations
- Different colours correspond to different total intensity offsets

# Polarization fractions and column density



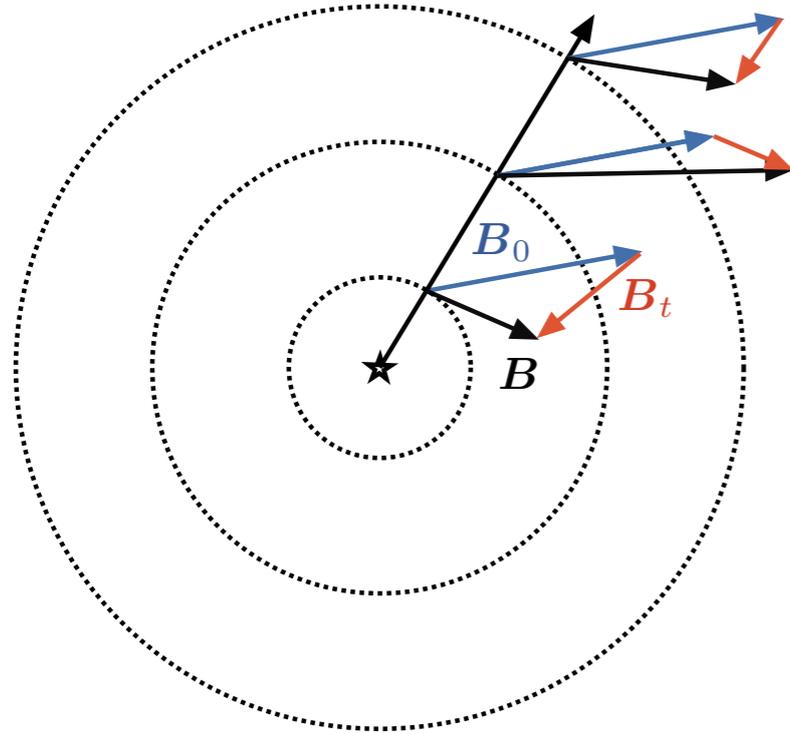
- Large scatter in the diffuse ISM
- Decrease of the polarization fraction towards more crowded or denser regions
- Low intensity end quite sensitive to offset : potential constraint ?

# Polarization fractions and angle dispersions



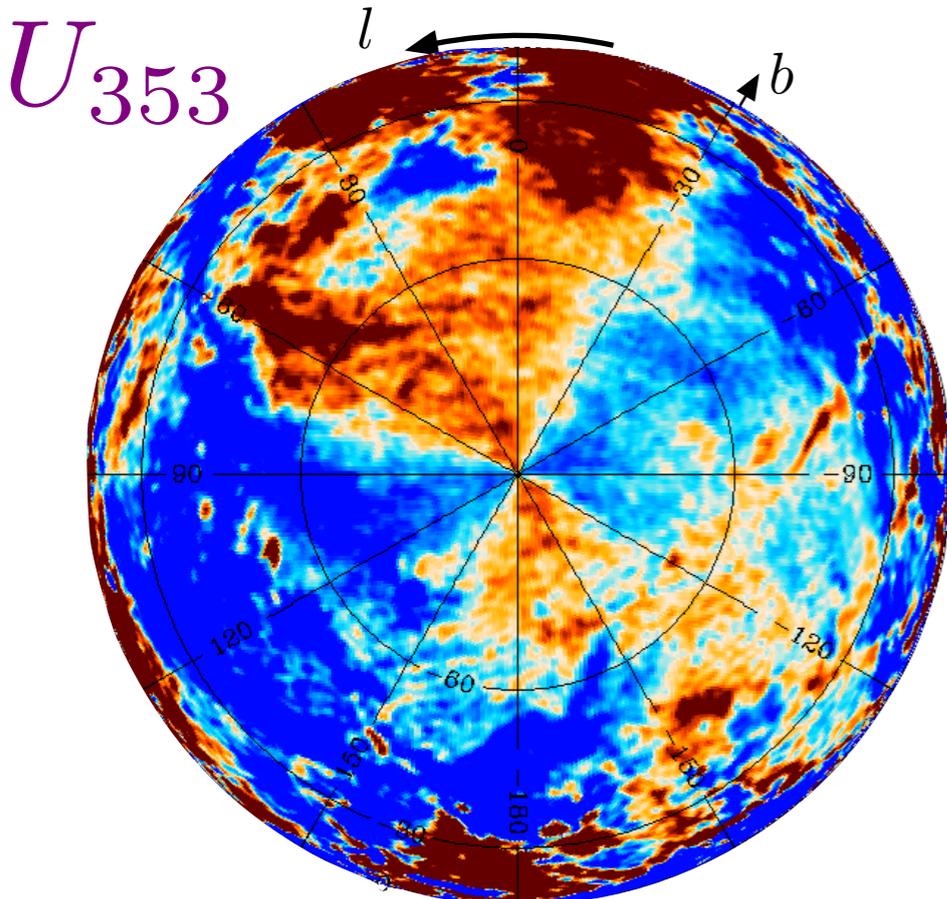
- Clear anti-correlation
- Consistent with findings of Planck Int. XIX (intermediate latitudes only)
- Reproduced by a simple phenomenological model

# A phenomenological model of the Planck polarized sky



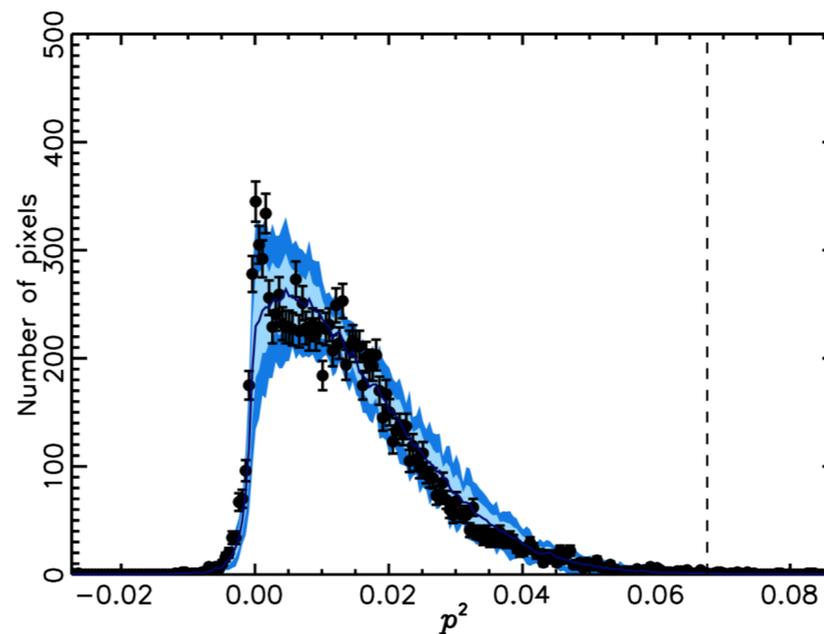
Magnetic field  $B = B_0 + B_t$   
 Uniform field Uniform field Turbulent field

- A superposition of variously polarized layers (turbulent cells ?)
- Turbulent field : 3D Gaussian random variable
- Analysis of the Southern Galactic cap
  - Spatial power spectrum unconstrained  $C_\ell \propto \ell^{\alpha_M}$
  - Direction of the large-scale field  $(l_0, b_0) = (70 \pm 5^\circ, 24 \pm 5^\circ)$
  - Turbulent-to-mean ratio  $f_M = 0.9 \pm 0.1$
  - Number of layers  $N = 7 \pm 2$
  - Intrinsic polarization fraction  $p_0 = 26 \pm 3\%$

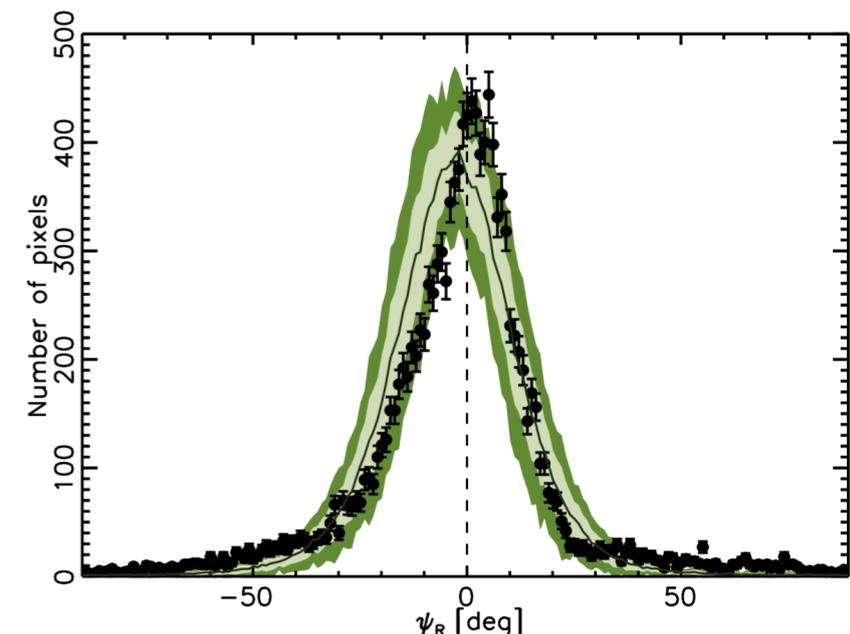


$U_{353}$

Observations (black dots) vs. Simulations (colored regions)



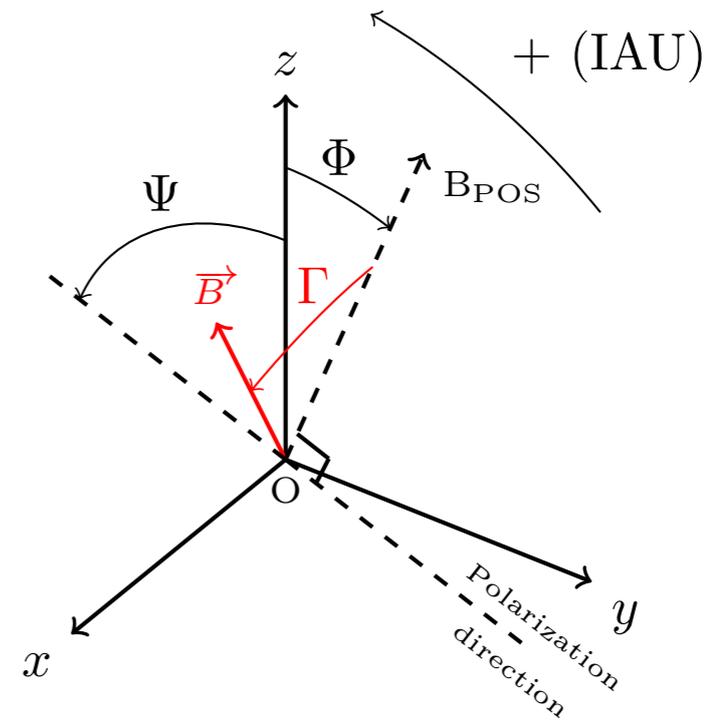
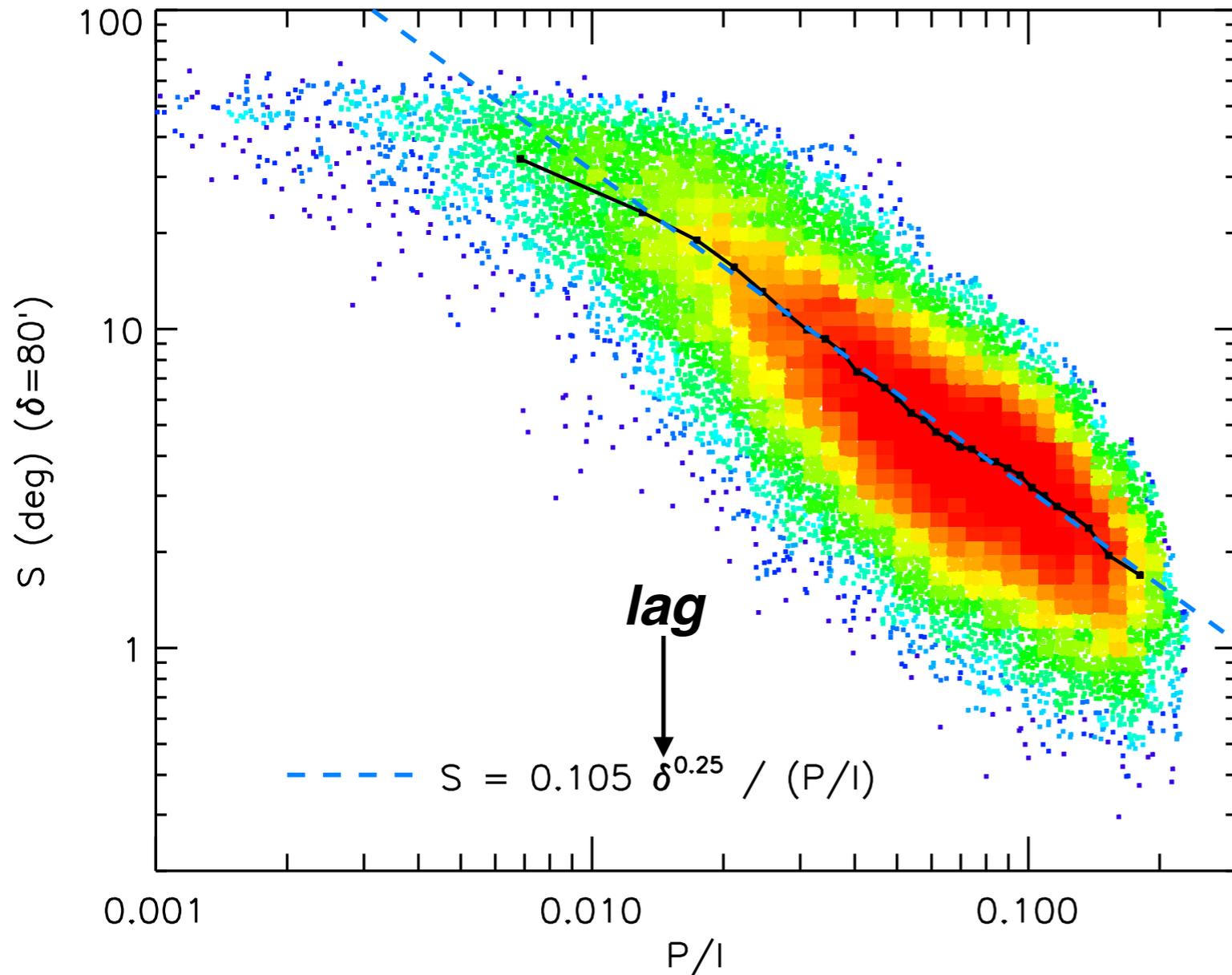
Polarization fraction



Polarization angle relative to the large-scale field

# Analytical derivation of the S vs p relation

S and p distribution in a model sky



$$\langle S(\ell) \rangle_p \simeq \frac{f_m(\ell)}{\sqrt{6N}} \frac{p_{\max}}{p}$$

where  $f_m(\ell) = \frac{\delta B}{B_i}$

Because changes of dust properties or dust alignment are not included in either the Gaussian models or the synthetic observations from MHD simulations, we conclude that the anti-correlation between  $S$  and  $p$  must be a generic statistical property that results quite simply from the topology of the magnetic field alone.



# Modelling polarized thermal dust emission with fBm fields

- Dust density and magnetic field modelled by 3D fields with realistic spatial correlations
- 9-parameter model (including spectral indices, fluctuation levels, angle of the mean field and depth on the LOS)
- Simulated polarization maps characterized by PDFs, power spectra, and correlations
- Monte-Carlo Markov Chain exploration of parameter likelihood given input polarization maps

## Model parameters

Parameter	Prior <sup>a</sup>	Definition
$\beta_B$	[1, 4]	Spectral index of the 3D turbulent magnetic field
$\beta_n$	[1, 5]	Spectral index of the 3D dust density field
$\log_{10} y_n$	[-1, 1]	Log of the RMS-to-mean ratio of dust density
$\log_{10} y_B^{\text{POS}}$	[-1, 1]	Log of the ratio of the turbulent magnetic field RMS to the mean magnetic field in the POS
$\chi_0$	[-90°, 90°]	Position angle of the mean magnetic field in the POS
$\log_{10} (d/1 \text{ pc})$	[-0.3, 1.5] <sup>b</sup>	Depth of the simulated cube
$\log_{10} (\langle n_H \rangle / 1 \text{ cm}^{-3})$	[1, 2.7] <sup>c</sup>	Mean dust density
$T_d$	[5 K, 200 K]	Dust temperature
$p_0$	[0.01, 0.5]	Intrinsic polarisation fraction parameter

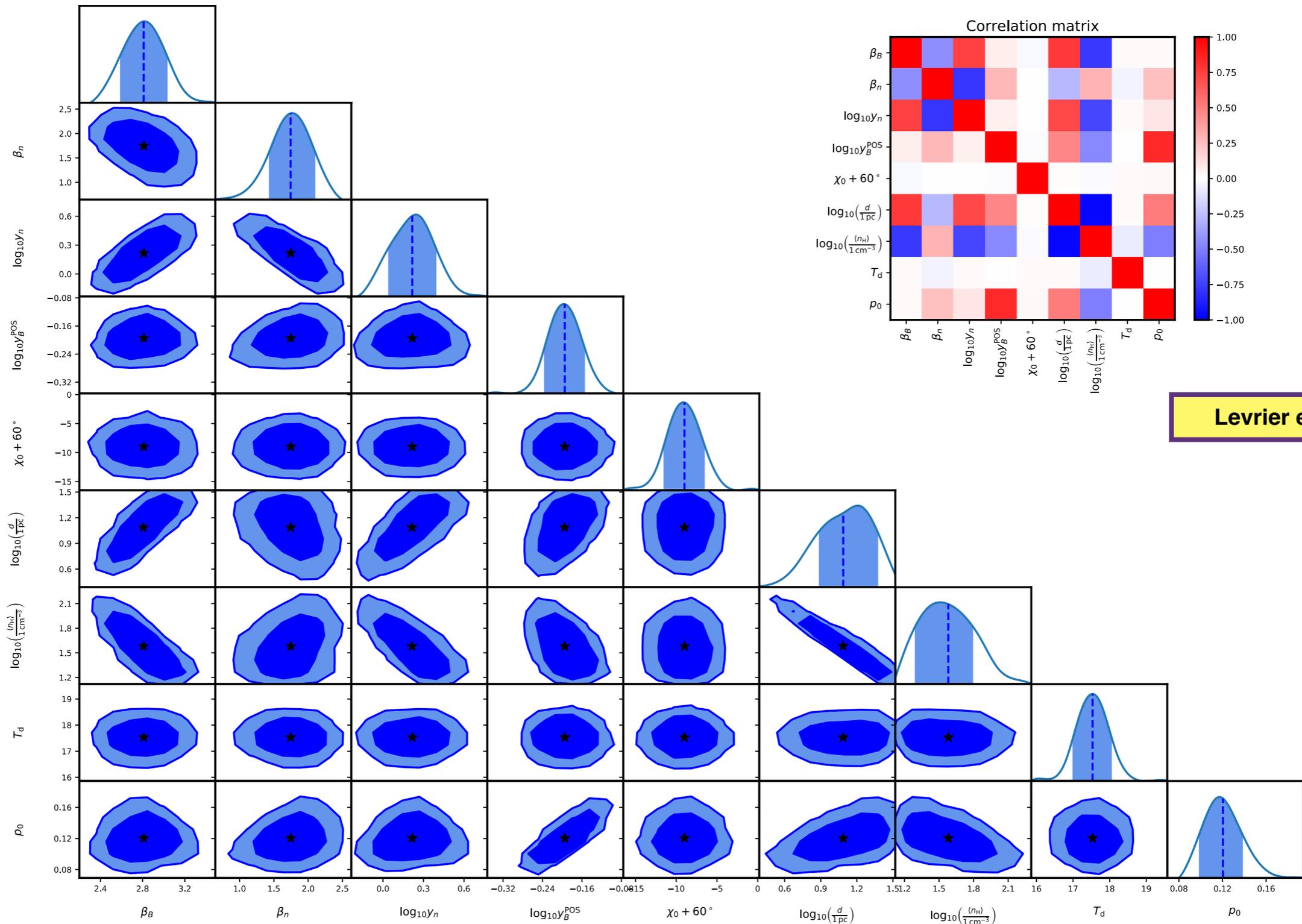
## Observables

Type	From
Mean values	$\tau_{353}, T_{\text{obs}}$
Distribution function	$I_m, Q_m, U_m, p_{\text{MAS}}, \psi, \mathcal{S}, \tau_{353} / \langle \tau_{353} \rangle$
Power spectrum	$I_m, Q_m, U_m$
Correlation	$\{\mathcal{S}, p_{\text{MAS}}\}$



# MCMC fitting on the Polaris Flare Planck polarization maps

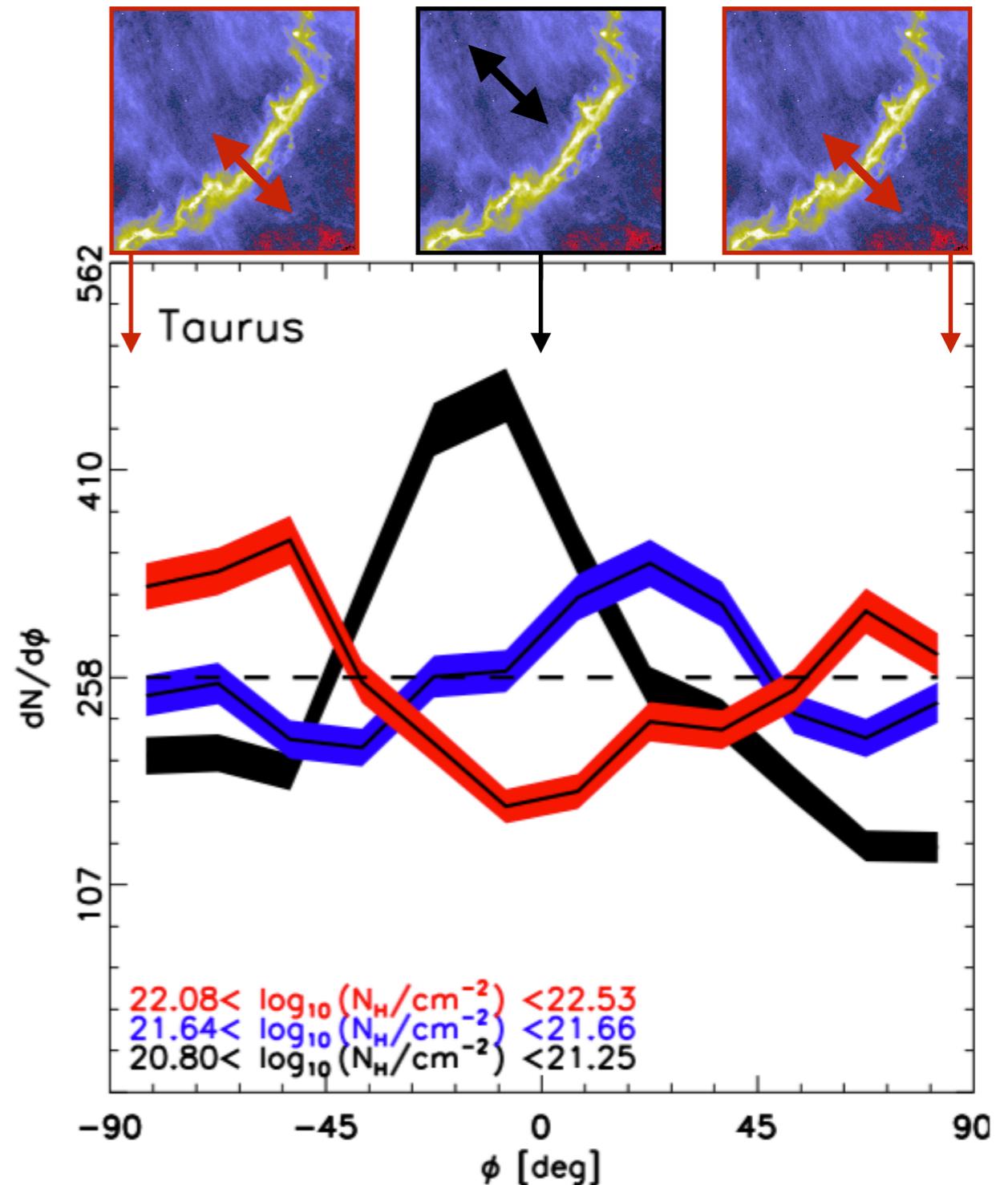
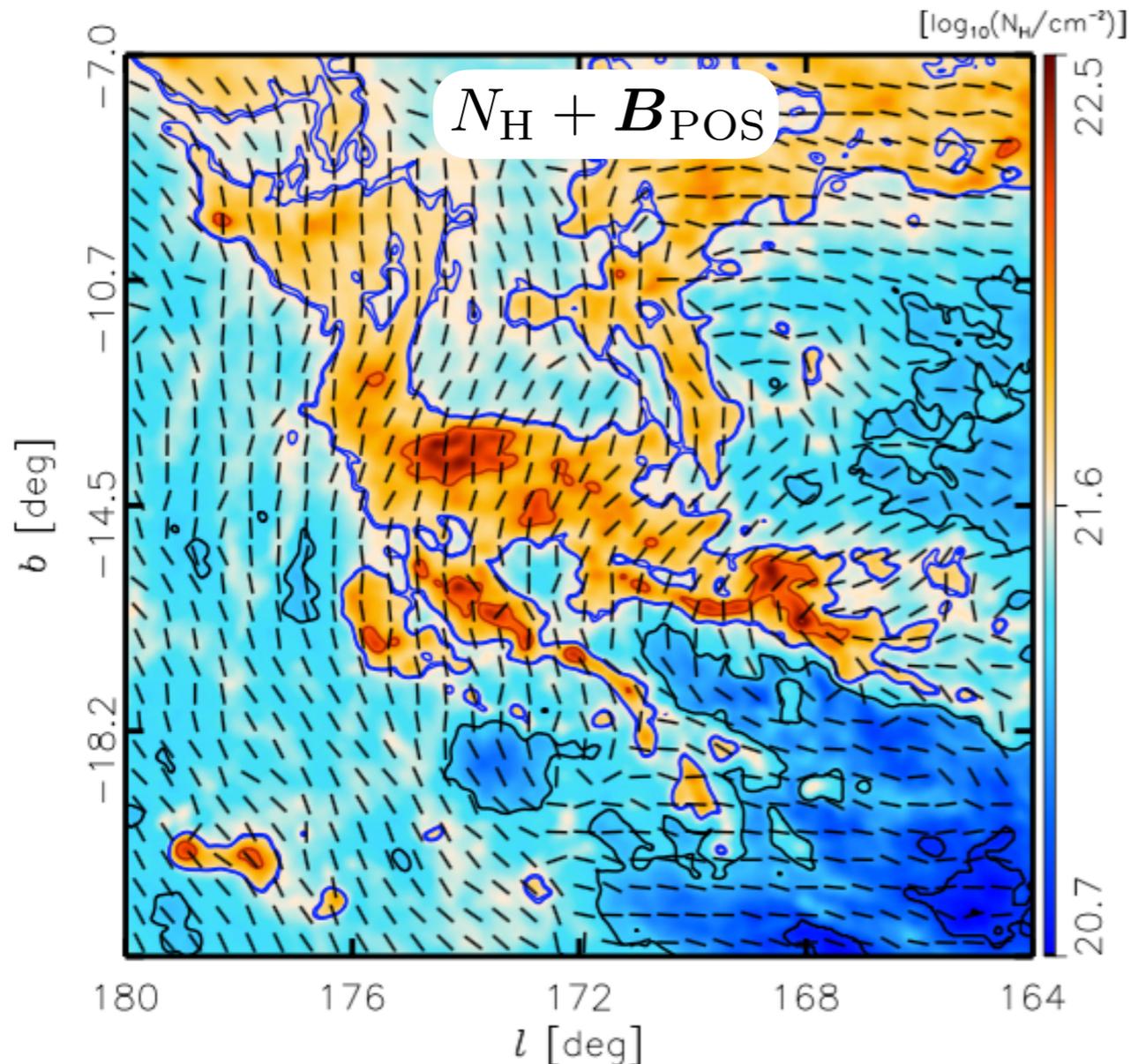
Parameters	$\beta_B$	$\beta_n$	$\log_{10} y_n$	$\log_{10} y_B^{\text{POS}}$	$\chi_0 [^\circ]$	$\log_{10} \left( \frac{d}{1 \text{ pc}} \right)$	$\log_{10} \left( \frac{\langle n_H \rangle}{1 \text{ cm}^{-3}} \right)$	$T_d \text{ [K]}$	$p_0$	$\langle \chi_{\text{best}}^2 \rangle$
Best fit values	<b><math>2.8^{+0.2}_{-0.2}</math></b>	$1.7^{+0.4}_{-0.3}$	$0.2^{+0.2}_{-0.2}$	$-0.19^{+0.04}_{-0.04}$	$-69^{+2}_{-3}$	$1.1^{+0.3}_{-0.2}$	$1.6^{+0.2}_{-0.3}$	$17.5^{+0.5}_{-0.5}$	$0.12^{+0.02}_{-0.02}$	2.9



# Orientation of magnetic field and structures of matter

- In nearby molecular clouds, using the Histogram of Relative Orientations (HRO) Soler et al. (2013)
- Change of relative orientation as column density increases
- Consistent with sub- and trans-Alfvénic simulations of MHD turbulence (strong magnetic field)
- Estimates of  $B$  from the Davis-Chandrasekhar-Fermi method Chandrasekhar & Fermi (1953), Hildebrand et al. (2009)

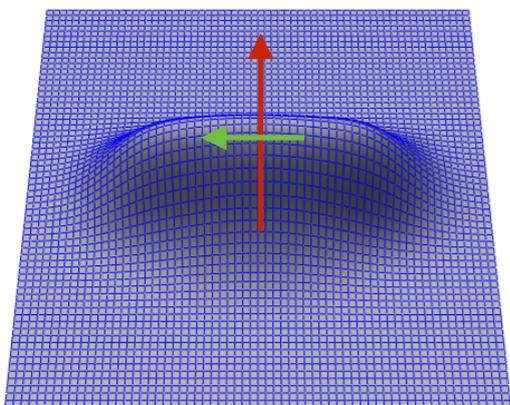
$$B_{\text{POS}} \sim 10 - 50 \mu\text{G}$$



# Orientation of magnetic field and structures of matter

- At intermediate and high Galactic latitudes, using the eigenvalues and eigenvectors of the Hessian
- Relative angle between filaments and magnetic field shows preferred alignment

$$\mathbf{H} = \begin{bmatrix} \partial_{xx}^2 D_{353} & \partial_{xy}^2 D_{353} \\ \partial_{xy}^2 D_{353} & \partial_{yy}^2 D_{353} \end{bmatrix}$$



$$\langle p \rangle = 12 \pm 1\%$$

Map of the most negative eigenvalue

